# Package 'stors'

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Description Fast and efficient sampling from general univariate probability density functions. Implements a rejection sampling approach designed to take advantage of modern CPU caches and minimise evaluation of the target density for most samples. Many standard densities are internally implemented in 'C' for high performance, with general user defined densities also supported. A paper describing the methodology will be released soon.
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build\_proposal

Build Proposal

## Description

Constructs the step optimized proposal density, squeezing function, and log-linear tail proposal for a user defined probability density function.

## Usage

```
build_proposal(
   f,
   modes,
   lower = -Inf,
   upper = Inf,
   h = NULL,
   h_prime = NULL,
   steps = NULL,
   proposal_range = NULL,
   theta = 0.1,
   target_sample_size = 1000,
   verbose = FALSE,
   ...
)
```

#### **Arguments**

A function which returns the (unnormalised) probability density function of the

target distribution. The first argument must be the value at which the pdf is to be evaluated. Additional arguments may be parameters of the distribution, which

should be specified by name in the ... arguments.

modes Numeric vector of modes of the density function.

lower Numeric scalar representing the lower bound of the target density. Default is

-Inf for unbounded lower support.

upper Numeric scalar representing the upper bound of the target density. Default is

Inf for unbounded upper support.

h An optional function which returns the (unnormalised) log-probability density

function of the target distribution. As for f the first argument must be the value at which the log-pdf is to be evaluated and additional parameters may be named

arguments passed to . . . .

h\_prime An optional function which returns the first derivative of the (unnormalised)

log-probability density function of the target distribution. As for f the first argument must be the value at which the log-pdf is to be evaluated and additional

parameters may be named arguments passed to . . . .

steps Optional integer scalar specifying the number of steps in the step optimised part

of the proposal density and squeezing function.

proposal\_range Optional numeric vector of length 2 specifying the lower and upper range of the

steps in the step optimised part of the proposal density and squeezing function. This range should be contained within the interval defined by lower and upper.

theta Optional numeric scalar (between 0.1 and 1) defining the pre-acceptance thresh-

old. This dictates when no further steps should be added in the step optimised part of the proposal density and squeezing function, based on the probability of

pre-acceptance.

target\_sample\_size

Integer scalar indicating the typical sample size that will be requested when sampling from this density using build\_sampler. The proposal optimization process bases benchmark timings on this target size in order to select a proposal best suited to the desired sample size. Note this does *not* limit sampling to this number, it is merely a guide should the user be aware that a certain sample size will

be most commonly sampled.

verbose Logical scalar. If TRUE, a table detailing the optimization areas and steps will be

displayed during proposal optimization. Defaults to FALSE.

Further arguments to be passed to f, h, and h\_prime, if they depend on addi-

tional parameters.

#### **Details**

This function is the starting point when a user wishes to build a custom sampler using StORS. It is responsible for generating the step optimized proposal density, squeezing function, and log-linear tail proposal that can be utilized for this purpose. The minimum information that must be supplied by the user is:

- The (closed) interval of support for the distribution, [lower, upper]  $\in \mathbb{R}$ , which may also be half-closed on either side, or all of  $\mathbb{R}$ .
- The probability density function (pdf), which need not be normalised, f.
- Any modes of the pdf, as vector modes.

Optionally, the log-pdf and derivative of the log-pdf may be supplied.

#### **Arguments for pdf**

The pdf (and log-pdf and first derivative of the log-pdf) may depend on certain parameters. If so, these can be from the second argument onward in f. For instance, consider the Kumaraswamy distribution, which has pdf:

$$f(x; a, b) = abx^{a-1}(1 - x^a)^{b-1}$$
, where  $x \in (0, 1)$ 

This pdf has known modes.

Then, to implement as a custom StORS sampler, we would first define the pdf in R:

dkumaraswamy <- function(x, a, b)  $a*b*(x^(a-1))*(1-x^a)^(b-1)$ 

Then, to construct a StORS proposal for a=2 and b=2, we would call

Proposal <- build\_Proposal(lower = 0, upper = 1, modes = sqrt(1/3), f = dkumaraswamy, a = 2, b = 2)

#### StORS proposal construction

StORS defines an unnormalised piecewise constant proposal density and squeezing function, with a Proposal defining the change points. To optimise the execution speed on modern CPUs, the unnormalised piecewise constant proposal has fixed area for each segment with one end of the segment coinciding with the user's pdf. That is, each step of the function has width defined by  $w_i = (x_i - x_{i-1})$  and a height determined by  $h_i = \max(f(x_{i-1}), f(x_i))$ , such that  $w_i h_i = \alpha \ \forall i$  where  $\alpha$  is constant.

Once the user has constructed the proposal, the sampling function can be built using build\_sampler().

#### Internal details

The function build\_final\_Proposal() manages the construction of these steps and calculates values critical for the sampling process. When the resultant Proposal is used with the build\_sampler() function, these values are cached, significantly enhancing the computational efficiency and hence improving sampling speed. During the optimization process, we aim for a certain Proposal size based on L1-3 memory cache size. Therefore, we test the speed of Proposals of sizes  $2^m$  Kb. To achieve this, we estimate the uniform step area based on a certain steps number that leads to the target cache size,  $\alpha = \frac{1}{\text{number of steps}}$ .

The speed testing for each possible Proposal is initially based on a sample size of 1000. However, if the user wishes to optimize the Proposal for a different sample size, they can do so by specifying the desired sample size using the target\_sample\_size argument.

In case the user wants to select a specific number of steps for the proposal and bypass the optimization process, this can be done by specifying a steps number greater than the number of modes by 2 using the steps argument. If the target density is heavy-tailed, and the user wishes to stop the Proposal building process at a certain pre-acceptance threshold, this can be achieved by setting the acceptance probability threshold theta  $\theta$ . Once the steps reach this level of pre-acceptance probability, the step construction will end  $\frac{\min(f(x_i), f(x_{i+1}))}{\max(f(x_i), f(x_{i+1}))} < \theta$ . Alternatively, if the user wishes to create the steps within certain limits on the x-axis, they can do so by specifying the proposal limits using the proposal\_range argument.

#### Value

This returns a list which is used to construct the sampler by passing to build\_sampler function.

A list containing the optimized proposal and related parameters for the specified built-in distribution:

data A data frame with detailed information about the proposal steps, including:

x The start point of each step on the x-axis.

s\_upper The height of each step on the y-axis.

p\_a Pre-acceptance probability for each step.

s\_upper\_lower A vector used to scale the uniform random number when the sample is accepted.

areas A numeric vector containing the areas under:

left\_tail The left tail bound.

steps The middle steps.

right\_tail The right tail bound.

steps\_number An integer specifying the number of steps in the proposal.

sampling\_probabilities A numeric vector with:

left\_tail The probability of sampling from the left tail.

left\_and\_middle The combined probability of sampling from the left tail and middle steps.

unif\_scaler A numeric scalar, the inverse probability of sampling from the steps part of the proposal  $(\frac{1}{p(lower < x < upper)})$ . Used for scaling uniform random values.

1t\_properties A numeric vector of 5 values required for Adaptive Rejection Sampling (ARS) in the left tail.

rt\_properties A numeric vector of 6 values required for ARS in the right tail.

alpha A numeric scalar representing the uniform step area.

tails\_method A string, either "ARS" (Adaptive Rejection Sampling) or "IT" (Inverse Transform), indicating the sampling method for the tails.

proposal\_bounds A numeric vector specifying the left and right bounds of the target density.

cnum An integer representing the cache number of the created proposal in memory.

symmetric A numeric scalar indicating the symmetry point of the proposal, or NULL if not symmetric.

f\_params A list of parameters for the target density that the proposal is designed for.

is\_symmetric A logical value indicating whether the proposal is symmetric.

proposal\_type A string indicating the type of the generated proposal:

"scaled" The proposal is "scalable" and standardized with rate = 1. This is used when parameter rate is either NULL or not provided. Scalable proposals are compatible with srexp.

"custom" The proposal is "custom" when rate is provided. Custom proposals are compatible with srexp\_custom.

target\_function\_area A numeric scalar estimating the area of the target distribution.

dens\_func A string containing the hardcoded density function.

density\_name A string specifying the name of the target density distribution.

lock An identifier used for saving and loading the proposal from disk.

#### See Also

build\_sampler: Function to build and return a sampling function based on the provided proposal properties.

```
# Example 1: Building a proposal for Standard Normal Distribution
# This example demonstrates constructing a proposal for a standard normal distribution
# \ (f(x) \sim \mathbb{N}(0,1) \),
# and shows the optimization table by setting \code{verbose} to \code{TRUE}.
# Define the density function, its logarithm,
# and its derivative for the standard normal distribution
modes norm = 0
f_{norm} \leftarrow function(x) \{ 1 / sqrt(2 * pi) * exp(-0.5 * x^2) \}
h_norm <- function(x) { log(f_norm(x)) }</pre>
h_prime_norm <- function(x) { -x }</pre>
# Following example takes slightly too long to run on CRAN.
# Build the proposal for the standard normal distribution
norm_proposal = build_proposal(lower = -Inf, upper = Inf, mode = modes_norm,
f = f_norm, h = h_norm, h_prime = h_prime_norm, verbose = TRUE)
# Plot the generated proposal
plot(norm_proposal)
# Example 2: proposal for a Bimodal Distribution
# This example shows how to build a proposal for sampling from a bimodal distribution,
#combining two normal distributions
\# (f(x) = 0.5 \cdot w_1(x) + 0.5 \cdot w_2(x) ),
# where ( w_1(x) \times \mathbb{N}(0, 1) ) and ( w_2(x) \times \mathbb{N}(0, 1) ).
# Define the bimodal density function
f_bimodal <- function(x) {</pre>
 0.5 * (1 / sqrt(2 * pi)) * exp(-(x^2) / 2) + 0.5 * (1 / sqrt(2 * pi)) * exp(-((x - 4)^2) / 2)
modes\_bimodal = c(0.00134865, 3.99865)
# Build the proposal for the bimodal distribution
bimodal_proposal = build_proposal( f = f_bimodal, lower = -Inf, upper = Inf, mode = modes_bimodal)
# Print and plot the bimodal proposal
print(bimodal_proposal)
plot(bimodal_proposal)
# Example 3: Proposal with 500 Steps for Bimodal Distribution
# This example demonstrates constructing a proposal with 500 steps,
# for the bimodal distribution used in Example 2.
bimodal_proposal_500 = build_proposal(f = f_bimodal, lower = -Inf, upper = Inf,
```

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```
mode = modes_bimodal, steps = 500)
# Print and plot the proposal with 500 steps
print(bimodal_proposal_500)
```

build\_sampler

Sampling Function for User Defined Density

## **Description**

This function generates a sampling function based on a proposal created by the user using the build\_proposal() function. The resulting sampling function can then be used to produce samples.

#### Usage

```
build_sampler(proposal)
```

#### **Arguments**

proposal

The sampling proposal created using the build\_proposal() function.

#### **Details**

After a user creates a proposal for their desired sampling function using build\_proposal, this proposal must be passed to build\_sampler() to create a sampling function for the target distribution. build\_sampler() first checks whether the proposal was indeed created using build\_proposal(). If the user has altered or modified the proposal returned from build\_proposal(), build\_sampler() will reject the altered proposal; therefore, no changes should be made to the proposal after its creation. Once the proposal is accepted by build\_sampler(), it is cached in memory, allowing fast access to proposal data for the compiled C code and reducing memory access latency. Subsequently, build\_sampler() returns a function that can be utilized to generate samples from the target distribution,

#### Value

Returns a function that can be used to generate samples from the specified proposal.

```
# Example 1
# To sample from a standard normal distribution \( f(x) \sim \mathcal{N}(0,1) \),
# first build the proposal using \code{build_proposal()}

modes_norm = 0
f_norm <- function(x) { 1 / sqrt(2 * pi) * exp(-0.5 * x^2) }
h_norm <- function(x) { log(f_norm(x)) }
h_prime_norm <- function(x) { -x }
normal_proposal = build_proposal(lower = -Inf, upper = Inf, mode = modes_norm,</pre>
```

```
f = f_norm, h = h_norm, h_prime = h_prime_norm, steps = 1000)
# Generate samples from the standard normal distribution
sample_normal <- build_sampler(normal_proposal)</pre>
hist(sample_normal(100), main = "Normal Distribution Samples")
# Example 2
# Let's consider a bimodal distribution composed of two normal distributions:
# The first normal distribution N(0,1) with weight p = 0.3,
# and the second normal distribution N(4,1) with weight q = 0.7.
f_bimodal <- function(x) {</pre>
0.3 * (1 / sqrt(2 * pi) * exp(-0.5 * (x - 0)^2)) +
0.7 * (1 / sqrt(2 * pi) * exp(-0.5 * (x - 4)^2))
# Define the modes of the bimodal distribution
  modes\_bimodal <- c(0.00316841, 3.99942)
# Build the proposal for the bimodal distribution
bimodal_proposal = build_proposal(f = f_bimodal, modes = modes_bimodal,
lower = -Inf, upper = Inf, steps = 1000)
# Create the sampling function using \code{build_sampler()}
sample_bimodal <- build_sampler(bimodal_proposal)</pre>
# Generate and plot samples from the bimodal distribution
bimodal_samples <- sample_bimodal(1000)</pre>
hist(bimodal_samples, breaks = 30, main = "Bimodal Distribution Samples")
# Create the truncated sampling function using
# \code{build_sampler()} with truncation bounds [-0.5, 6]
truncated_bimodal_proposal <- build_proposal(f = f_bimodal,</pre>
modes = modes_bimodal, lower = -0.5, upper = 6, steps = 1000)
# Create the sampling function using \code{build_sampler()}
sample_truncated_bimodal <- build_sampler(truncated_bimodal_proposal)</pre>
# Generate and plot samples from the truncated bimodal distribution
truncated_sample <- sample_truncated_bimodal(1000)</pre>
hist(truncated_sample, breaks = 30, main = "Truncated Bimodal Distribution Samples")
```

## **Description**

This function deletes built-in proposals from disk by specifying the sampling function and proposal type. It is useful for managing cached proposals and freeing up storage space.

#### Usage

```
delete_built_in_proposal(sampling_function, proposal_type = "custom")
```

## **Arguments**

```
sampling_function
String. The name of the sampling distribution's function in STORS. For example, "srgamma" or "srchisq".

proposal_type String. Either "custom" to delete the custom proposal or "scaled" to delete the scaled proposal. Defaults to "custom".
```

#### **Details**

The function looks for the specified proposal type associated with the sampling function in the built-in proposals directory. If the proposal exists, it deletes the corresponding proposal file from disk and frees its cached resources. If the specified sampling function or proposal type does not exist, an error is thrown.

#### Value

A message indicating the status of the deletion process, or an error if the operation fails.

```
# The following examples are not run, since if they are run the srgamma and
# srnorm samplers will no longer work until a new grid is built for them.
# This causes problems if the examples are run by CRAN checks or the website
# build system.
## Not run:
# Delete a custom proposal for the srgamma function (uncomment to run)
delete_built_in_proposal(sampling_function = "srgamma", proposal_type = "custom")
# Delete a scaled proposal for the srnorm function (uncomment to run)
delete_built_in_proposal(sampling_function = "srnorm", proposal_type = "scaled")
## End(Not run)
```

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delete\_proposal

Delete Proposal

#### **Description**

This function deletes a proposal that was previously stored by the user using the save\_proposal() function. It is useful for managing stored proposals and freeing up space.

#### Usage

```
delete_proposal(proposal_name)
```

## **Arguments**

proposal\_name A string specifying the name of the proposal to be deleted.

#### Value

If proposal\_name does not exist, the function returns an error message. If the proposal exists and is successfully deleted, a message confirming its successful removal will be displayed.

```
# First, let's create a proposal to sample from a standard normal distribution
f_normal <- function(x) { 0.3989423 * exp(-0.5 * x^2) }
normal_proposal = build_proposal(f = f_normal, modes = 0, lower = -Inf, upper = Inf, steps = 1000)
print(normal_proposal)

# Then, save this proposal in R's internal data directory using
# `save_proposal()` with the name "normal"
save_proposal(normal_proposal, "normal")

# Now, we can print all proposals stored on this machine using `print_proposals()`
print_proposals()

# The list will include the `normal_proposal` stored under the name "normal"

# To delete the "normal" proposal from the machine, pass its name to `delete_proposal`
delete_proposal("normal")

# Now, when we print all stored proposals, the "normal" proposal will no longer be listed
print_proposals()</pre>
```

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load\_proposal Load Stored Proposal

## Description

This function loads a proposal into memory that was previously saved using the save\_proposal() function. It is useful for retrieving saved proposals for further analysis or processing.

## Usage

```
load_proposal(proposal_name)
```

## **Arguments**

proposal\_name A string specifying the name of the proposal to be loaded.

#### Value

Returns a list representing the proposal stored under proposal\_name in R's internal data directory. If the proposal corresponding to the specified name does not exist, an error message is displayed.

#### **Examples**

```
# First, let's create a proposal to sample from a standard normal distribution
f_normal <- function(x) { 0.3989423 * exp(-0.5 * x^2) }
normal_proposal = build_proposal(f = f_normal, modes = 0, lower = -Inf, upper = Inf, steps = 1000)
print(normal_proposal)

# Then, save this proposal in R's internal data directory using
# `save_proposal()` with the name "normal"
save_proposal(normal_proposal, "normal")

# Now, in case the R session is restarted and the proposal is no longer in memory,
# it can be loaded from the machine as follows:
loaded_normal_proposal <- load_proposal("normal")
print(loaded_normal_proposal)</pre>
```

plot.proposal

Plot Method for Proposal Objects

#### **Description**

This function evaluates the properties of the included target and proposal functions to create a plot for both functions. In cases where the proposal function's steps part is too dense, x\_min and x\_max can be set to crop and scale the chart for better visualization.

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## Usage

```
## S3 method for class 'proposal'
plot(x, x_min = NA, x_max = NA, ...)
```

#### **Arguments**

X	A list generated using STORS' build_proposal() or proposal_optimizer() functions.
x_min	A scalar that represents the left cropping of the chart on the x-axis.
x_max	A scalar that represents the right cropping of the chart on the x-axis.
	Additional arguments passed to the plot function.

#### **Details**

This method extends the generic plot() function for objects of class proposal. It offers custom plotting functionality specifically designed for visualizing proposal objects.

#### Value

A plot of the target density and proposal. If ggplot2 is available, it returns a ggplot object representing the plot. otherwise, it uses the base plot() function.

#### See Also

```
print.proposal
```

```
# Define the density function, its logarithm,
# and its derivative for the standard normal distribution
modes_norm = 0
f_norm <- function(x) { 1 / sqrt(2 * pi) * exp(-0.5 * x^2) }
h_norm <- function(x) { log(f_norm(x)) }
h_prime_norm <- function(x) { -x }

# Build a dense proposal for the standard normal distribution
norm_proposal = build_proposal(lower = -Inf, upper = Inf, mode = modes_norm,
    f = f_norm, h = h_norm, h_prime = h_prime_norm, steps = 4000)

# Plot the generated proposal
plot(norm_proposal)

# To visualize the proposal in a cropped area between -0.1 and 0
plot(norm_proposal, x_min = -0.1, x_max = 0)</pre>
```

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#### **Description**

The function displays detailed information about the proposal object created by STORS' build\_proposal() or proposal\_optimizer() functions. This includes the number of steps within the proposal, the range of values covered by the proposal, and the proposal's sampling efficiency. This information is crucial for understanding the structure and performance of the proposal in sampling processes.

#### Usage

```
## S3 method for class 'proposal'
print(x, ...)
```

#### **Arguments**

- x A list generated using STORS' build\_proposal() or proposal\_optimizer() functions.
- ... Additional arguments passed to the print function.

## **Details**

This method extends the generic print function for objects of class proposal. It prints the provided proposal's features such as the number of steps, steps limit, and efficiency.

## Value

Prints a summary of the proposal's properties, but does not return any value.

```
# Define the density function, its logarithm,
#and its derivative for the standard normal distribution
modes_norm = 0
f_norm <- function(x) { 1 / sqrt(2 * pi) * exp(-0.5 * x^2) }
h_norm <- function(x) { log(f_norm(x)) }
h_prime_norm <- function(x) { -x }

# Build a dense proposal for the standard normal distribution
norm_proposal = build_proposal(lower = -Inf, upper = Inf, mode = modes_norm,
    f = f_norm, h = h_norm, h_prime = h_prime_norm, steps = 1000)

# Print the properties of the generated proposal
print(norm_proposal)</pre>
```

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print\_proposals

Print proposals

#### **Description**

This function prints details of all proposals stored by the user. It provides information on each proposal, including the proposal name, size, efficiency, and other relevant details.

## Usage

```
print_proposals()
```

#### Value

Prints a summary of all proposals, but does not return any value.

```
# First, let's create a proposal to sample from a standard normal distribution
f_{normal} \leftarrow function(x) \{ 0.3989423 * exp(-0.5 * x^2) \}
normal_proposal = build_proposal(f = f_normal, modes = 0, lower = -Inf, upper = Inf, steps = 1000)
print(normal_proposal)
# `print_proposals()` prints all proposals stored in R's internal data directory.
# To see this, we first save `normal_proposal` using `save_proposal()`
save_proposal(normal_proposal, "normal")
# Since `normal_proposal` is now stored on this machine,
# we can confirm this by printing all saved proposals
print_proposals()
# Example 2: Create and Save a proposal for a Bimodal Distribution
f_bimodal <- function(x) {</pre>
  0.5 * (1 / sqrt(2 * pi)) * exp(-(x^2) / 2) +
  0.5 * (1 / sqrt(2 * pi)) * exp(-((x - 4)^2) / 2)
}
modes\_bimodal = c(0, 4)
bimodal_proposal = build_proposal(f = f_bimodal, modes = modes_bimodal,
lower = -Inf, upper = Inf, steps = 1000)
save_proposal(bimodal_proposal, "bimodal")
print(bimodal_proposal)
# To print all stored proposals after saving bimodal_proposal
print_proposals()
```

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|--|--|

## **Description**

This function stores proposals generated by the build\_proposal() function in R's internal data directory. It is useful when users want to reuse a proposal across multiple R sessions.

## Usage

```
save_proposal(proposal, proposal_name)
```

## **Arguments**

proposal list representing an optimized proposal generated using the build\_proposal()

function.

proposal\_name string specifying the name under which the proposal will be saved.

#### Value

This function will produce an error if the proposal is not generated by the build\_proposal() function. Otherwise, it successfully saves the proposal without returning any value upon completion.

```
# First, let's create a proposal to sample from a standard normal distribution
f_normal <- function(x) { 0.3989423 * exp( -0.5 * x^2) }
normal_proposal = build_proposal(f = f_normal, modes = 0, lower = -Inf, upper = Inf, steps = 1000)
print(normal_proposal)

# Then, we can save this proposal in R's internal data directory using `save_proposal()`
# with the name "normal"
save_proposal(normal_proposal, "normal")

# To make sure the `normal_proposal` has been stored in R's internal data directory,
# we can print all saved proposals using `print_proposals()`
print_proposals()</pre>
```

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srbeta\_custom

Sampling from Beta Distribution

#### Description

The srbeta\_custom() function generates random samples from a Beta distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Adaptive Rejection Sampling (ARS) for the tails.

## Usage

```
srbeta\_custom(n = 1, x = NULL)
```

## **Arguments**

n Integer, length 1. Number of samples to draw.

x (optional) Numeric vector of length n. If provided, this vector is overwritten in place to avoid any memory allocation.

#### **Details**

The Beta Distribution

The Beta distribution has the probability density function (PDF):

$$f(x|\alpha,\beta) = \frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}, \quad 0 \le x \le 1,$$

where:

 $\alpha$  is the first shape parameter ( $\alpha > 0$ ).

 $\beta$  is the second shape parameter ( $\beta > 0$ ).

The Beta distribution is widely used in Bayesian statistics and in modelling probabilities and proportions.

#### Value

A numeric vector of length n containing random samples from the Beta distribution. The shape1 and shape2 parameters are specified during the optimization process using srbeta\_optimize().

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

## **TODO:** This density instead of this function.

This function samples from a proposal constructed using srbeta\_optimize, employing the STORS algorithm.

By default, srbeta\_custom() samples from the standard Beta distribution with shape1 = 1 and shape2 = 1. The proposal distribution is pre-optimized at package load time using srbeta\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

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## Note

This function is not scalable. Therefore, only the srbeta\_custom() version is available, which requires the proposal to be pre-optimized using srbeta\_optimize() before calling this function.

#### See Also

srbeta\_optimize to optimize the custom proposal.

## **Examples**

```
# Generate 10 samples from Beta Distribution
samples <- srbeta_custom(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srbeta_custom(10, x = x)
print(x)</pre>
```

srbeta\_optimize

Optimizing Beta Distribution proposal

## **Description**

The srbeta\_optimize() function generates an optimized proposal for a targeted Beta distribution. The proposal can be customized and adjusted based on various options provided by the user.

#### Usage

```
srbeta_optimize(
    shape1 = 2,
    shape2 = 2,
    xl = 0,
    xr = 1,
    steps = NULL,
    proposal_range = NULL,
    theta = 0.1,
    target_sample_size = 1000,
    verbose = FALSE
)
```

#### **Arguments**

shape 1 (optional) Numeric. The first shape parameter  $(\alpha)$  of the Beta distribution. De-

faults to 1.

shape 2 (optional) Numeric. The second shape parameter  $(\beta)$  of the Beta distribution.

Defaults to 1.

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	xl	Numeric. Left truncation bound for the target distribution. Defaults to $\emptyset$ , as the Beta distribution is defined only on the interval $[0, 1]$ .
	xr	Numeric. Right truncation bound for the target distribution. Defaults to 1, as the Beta distribution is defined only on the interval $[0, 1]$ .
	steps	(optional) Integer. Desired number of steps in the proposal. Defaults to 4091.
	proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to $NULL$ , indicating automatic range selection.
	theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.
target_sample_size		
		(optional) Integer. Target sample size for proposal optimization. Defaults to 1000.
	verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.

#### **Details**

When srbeta\_optimize() is explicitly called:

- A proposal is created and cached. If no parameters are provided, a standard proposal is created with shape1 = 1 and shape2 = 1.
- Providing shape1 and shape2 creates a custom proposal, which is cached for use with srbeta\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the target\_sample\_size.

## Value

A list containing the optimized proposal and related parameters for the specified Beta distribution. The proposal is also cached for internal use.

```
data Detailed information about the proposal steps, including x, s_{upper}, p_a, and s_{upper}lower. areas The areas under the left tail, steps, and right tail of the proposal distribution. steps_number The number of steps in the proposal.
```

f\_params The parameters (shape1 and shape2) of the Beta distribution.

#### See Also

srbeta\_custom: Function to sample from a custom proposal generated by srbeta\_optimize().

```
# Generate a standard proposal with shape1 = 1 and shape2 = 1
standard_proposal <- srbeta_optimize()

# Generate a custom proposal with shape1 = 2 and shape2 = 3
custom_proposal <- srbeta_optimize(shape1 = 2, shape2 = 3)</pre>
```

srchisq\_custom 19

srchisq\_custom

Sampling from Chi-squared Distribution

#### Description

The srchisq\_custom() function generates random samples from a Chi-squared Distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Adaptive Rejection Sampling (ARS) for the tails.

#### Usage

```
srchisq\_custom(n = 1, x = NULL)
```

#### **Arguments**

n Integer, length 1. Number of samples to draw.

x (optional) Numeric vector of length n. If provided, this vector is over written in place to avoid any memory allocation.

#### **Details**

The Chi-squared Distribution

The Chi-squared distribution has the probability density function (PDF):

$$f(x|k) = \frac{1}{2^{k/2}\Gamma(k/2)} x^{(k/2)-1} \exp(-x/2), \quad x \ge 0,$$

where:

k is the degrees of freedom (k > 0), which determines the shape of the distribution.

The Chi-squared distribution is widely used in hypothesis testing and constructing confidence intervals, particularly in the context of variance estimation.

this function is sampling from proposal that has been constructed using srchisq\_optimize, using the STORS algorithm.

By default, srchisq\_custom() samples from Chi-squared Distribution df = 2. The proposal distribution is pre-optimized at package load time using srchisq\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

## Value

A numeric vector of length n containing random samples from the Chi-squared distribution. The degrees of freedom (df) for the distribution are specified during the optimization process using srchisq\_optimize(). **NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

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## Note

This function is not scalable. Therefore, only the srchisq\_custom() version is available, which requires the proposal to be pre-optimized using srchisq\_optimize() before calling this function.

#### See Also

srchisq\_optimize to optimize the custom proposal.

#### **Examples**

```
# Genedf 10 samples from Chi-squared Distribution
samples <- srchisq_custom(10)
print(samples)

# Genedf 10 samples using a pre-allocated vector
x <- numeric(10)
srchisq_custom(10, x = x)
print(x)</pre>
```

srchisq\_optimize

Optimizing Chi-squared Distribution proposal

## **Description**

The srchisq\_optimize() function generates an optimized proposal for a targeted Chi-squared Distribution. The proposal can be customized and adjusted based on various options provided by the user.

## Usage

```
srchisq_optimize(
  df = 2,
  xl = NULL,
  xr = NULL,
  steps = 4091,
  proposal_range = NULL,
  theta = 0.1,
  target_sample_size = 1000,
  verbose = FALSE
)
```

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## Arguments

df	(optional) Numeric. degrees of freedom parameter of the Chi-squared Distribution. Defaults to NULL, which implies proposal with df = 2.	
xl	Numeric. Left truncation bound for the target distribution. Defaults to ${\sf -Inf}$ , representing no left truncation.	
xr	Numeric. Right truncation bound for the target distribution. Defaults to Inf, representing no right truncation.	
steps	(optional) Integer. Desired number of steps in the proposal. Defaults to NULL, which means the number of steps is determined automatically during optimization.	
proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to $NULL$ , indicating automatic range selection.	
theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.	
target_sample_size		
	(optional) Integer. Target sample size for proposal optimization. Defaults to 1000.	
verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.	

#### **Details**

When srchisq\_optimize() is explicitly called:

- A proposal is created and cached. If no parameters are provided, a standard proposal is created with df = 2.
- Providing df creates a custom proposal, which is cached for use with srchisq\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the. target\_sample\_size.

## Value

The user does not need to store the returned value, because the package internally cashes the proposal. However, we explain here the full returned proposal for advanced users.

A list containing the optimized proposal and related parameters for the specified built-in distribution:

data A data frame with detailed information about the proposal steps, including:

- x The start point of each step on the x-axis.
- s\_upper The height of each step on the y-axis.
- p\_a Pre-acceptance probability for each step.
- s\_upper\_lower A vector used to scale the uniform random number when the sample is accepted.

areas A numeric vector containing the areas under:

left\_tail The left tail bound.

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```
steps The middle steps.
```

right\_tail The right tail bound.

steps\_number An integer specifying the number of steps in the proposal.

sampling\_probabilities A numeric vector with:

left\_tail The probability of sampling from the left tail.

left\_and\_middle The combined probability of sampling from the left tail and middle steps.

unif\_scaler A numeric scalar, the inverse probability of sampling from the steps part of the proposal  $(\frac{1}{p(lower < x < upper)})$ . Used for scaling uniform random values.

1t\_properties A numeric vector of 5 values required for Adaptive Rejection Sampling (ARS) in the left tail.

rt\_properties A numeric vector of 6 values required for ARS in the right tail.

alpha A numeric scalar representing the uniform step area.

tails\_method A string, either "ARS" (Adaptive Rejection Sampling) or "IT" (Inverse Transform), indicating the sampling method for the tails.

proposal\_bounds A numeric vector specifying the left and right bounds of the target density.

cnum An integer representing the cache number of the created proposal in memory.

symmetric A numeric scalar indicating the symmetry point of the proposal, or NULL if not symmetric.

f\_params A list of parameters for the target density that the proposal is designed for.

df the df of the target distribution.

is\_symmetric A logical value indicating whether the proposal is symmetric.

proposal\_type A string indicating the type of the genedfd proposal:

"custom" The proposal is "custom" when df is provided. Custom proposals are compatible with srchisq\_custom.

target\_function\_area A numeric scalar estimating the area of the target distribution.

dens\_func A string containing the hardcoded density function.

density\_name A string specifying the name of the target density distribution.

lock An identifier used for saving and loading the proposal from disk.

#### See Also

srchisq\_custom: Function to sample from a custom proposal genedfd by srchisq\_optimize().

```
# Genedf custom proposal that with df = 2, that has 4096 steps
scalable_proposal <- srchisq_optimize(steps = 4096)

# Genedf custom proposal that with df = 4
scalable_proposal <- srchisq_optimize(df = 4)</pre>
```

srexp 23

Sampling from Exponential Distribution

#### **Description**

The srexp() function generates random samples from a Exponential Distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Inverse Transform (IT) method for the tails.

#### Usage

```
srexp(n = 1, rate = 1, x = NULL)

srexp\_custom(n = 1, x = NULL)
```

## **Arguments**

n	Integer, length 1. Number of samples to draw.
rate	Numeric. is the rate parameter of the Exponential Distribution.
x	(optional) Numeric vector of length $n$ . If provided, this vector is over written in
	place to avoid any memory allocation.

## **Details**

The Exponential distribution has the probability density function (PDF):  $f(x|\lambda) = \lambda \exp(-\lambda x), \quad x \ge 0$ , where:

 $\lambda$  is the rate parameter ( $\lambda > 0$ ), which determines the rate of decay of the distribution.

The Exponential distribution is commonly used to model the time between independent events that occur at a constant average rate.

These two functions are for sampling using the STORS algorithm based on the proposal that has been constructed using srexp\_optimize.

By default, srexp() samples from a standard Exponential Distribution rate = 1. The proposal distribution is pre-optimized at package load time using srexp\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

If srexp() is called with custom rate parameter, the samples are generated from the standard Exponential Distribution, then scaled accordingly.

## Value

A numeric vector of length n containing samples from the Exponential Distribution with the specified rate.

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

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#### See Also

srexp\_optimize to optimize the custom or the scaled proposal.

#### **Examples**

```
# Generate 10 samples from the standard Exponential Distribution
samples <- srexp(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srexp(10, x = x)
print(x)

# Generate 10 samples from a Exponential Distribution with rate = 4
samples <- srexp(10, rate = 4)
print(samples)</pre>
```

srexp\_optimize

Optimizing Exponential Distribution proposal

## **Description**

The srexp\_optimize() function generates an optimized proposal for a targeted Exponential Distribution. The proposal can be customized and adjusted based on various options provided by the user.

## Usage

```
srexp_optimize(
  rate = NULL,
  xl = NULL,
  xr = NULL,
  steps = 4091,
  proposal_range = NULL,
  theta = 0.1,
  target_sample_size = 1000,
  verbose = FALSE
)
```

## Arguments

x1

rate (optional) Numeric. rate parameter of the Exponential Distribution. Defaults to NULL, which implies a scalable proposal with rate = 1.

Numeric. Left truncation bound for the target distribution. Defaults to -Inf, representing no left truncation.

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xr Numeric. Right truncation bound for the target distribution. Defaults to Inf,

representing no right truncation.

steps (optional) Integer. Desired number of steps in the proposal. Defaults to NULL,

which means the number of steps is determined automatically during optimiza-

tion.

proposal\_range (optional) Numeric vector. Specifies the range for optimizing the steps part of

the proposal. Defaults to NULL, indicating automatic range selection.

theta Numeric. A parameter for proposal optimization. Defaults to 0.1.

target\_sample\_size

(optional) Integer. Target sample size for proposal optimization. Defaults to

1000.

verbose Boolean. If TRUE, detailed optimization information, including areas and steps,

will be displayed. Defaults to FALSE.

#### **Details**

When srexp\_optimize() is explicitly called:

 A proposal is created and cached. If no parameters are provided, a standard proposal is created with rate = 1.

- Providing rate creates a custom proposal, which is cached for use with srexp\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the. target\_sample\_size.

#### Value

The user does not need to store the returned value, because the package internally cashes the proposal. However, we explain here the full returned proposal for advanced users.

A list containing the optimized proposal and related parameters for the specified built-in distribution:

data A data frame with detailed information about the proposal steps, including:

x The start point of each step on the x-axis.

s\_upper The height of each step on the y-axis.

p\_a Pre-acceptance probability for each step.

s\_upper\_lower A vector used to scale the uniform random number when the sample is accepted.

areas A numeric vector containing the areas under:

left\_tail The left tail bound.

steps The middle steps.

right\_tail The right tail bound.

steps\_number An integer specifying the number of steps in the proposal.

sampling\_probabilities A numeric vector with:

left\_tail The probability of sampling from the left tail.

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left\_and\_middle The combined probability of sampling from the left tail and middle steps.

unif\_scaler A numeric scalar, the inverse probability of sampling from the steps part of the proposal  $(\frac{1}{p(lower < x < upper)})$ . Used for scaling uniform random values.

1t\_properties A numeric vector of 5 values required for Adaptive Rejection Sampling (ARS) in the left tail.

rt\_properties A numeric vector of 6 values required for ARS in the right tail.

alpha A numeric scalar representing the uniform step area.

tails\_method A string, either "ARS" (Adaptive Rejection Sampling) or "IT" (Inverse Transform), indicating the sampling method for the tails.

proposal\_bounds A numeric vector specifying the left and right bounds of the target density.

cnum An integer representing the cache number of the created proposal in memory.

symmetric A numeric scalar indicating the symmetry point of the proposal, or NULL if not symmetric.

f\_params A list of parameters for the target density that the proposal is designed for.

rate the rate of the target distribution.

is\_symmetric A logical value indicating whether the proposal is symmetric.

proposal\_type A string indicating the type of the generated proposal:

"scaled" The proposal is "scalable" and standardized with rate = 1. This is used when parameter rate is either NULL or not provided. Scalable proposals are compatible with srexp.

"custom" The proposal is "custom" when rate is provided. Custom proposals are compatible with srexp\_custom.

target\_function\_area A numeric scalar estimating the area of the target distribution.

dens\_func A string containing the hardcoded density function.

density\_name A string specifying the name of the target density distribution.

lock An identifier used for saving and loading the proposal from disk.

#### See Also

srexp: Function to sample from a scalable proposal generated by srexp\_optimize(). srexp\_custom:
Function to sample from a custom proposal tailored to user specifications.

```
# Generate scalable proposal that with rate = 1, that has 4096 steps
scalable_proposal <- srexp_optimize(steps = 4096)

# Generate custom proposal that with rate = 4
scalable_proposal <- srexp_optimize(rate = 4)</pre>
```

srgamma\_custom 27

srgamma\_custom

Sampling from Gamma Distribution

#### **Description**

The srgamma\_custom() function generates random samples from a Gamma distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Adaptive Rejection Sampling (ARS) for the tails.

#### Usage

```
srgamma_custom(n = 1, x = NULL)
```

#### **Arguments**

n Integer, length 1. Number of samples to draw.

x (optional) Numeric vector of length n. If provided, this vector is overwritten in place to avoid any memory allocation.

#### **Details**

The Gamma Distribution

The Gamma distribution has the probability density function (PDF):

$$f(x|\alpha,\beta) = \frac{\beta^{\alpha}}{\Gamma(\alpha)} x^{\alpha-1} \exp(-\beta x), \quad x \ge 0,$$

where:

 $\alpha$  is the shape parameter ( $\alpha > 0$ ), which determines the shape of the distribution.

 $\beta$  is the rate parameter ( $\beta > 0$ ), which determines the rate of decay.

The Gamma distribution is widely used in statistics, particularly in Bayesian inference and modelling waiting times.

This function samples from a proposal constructed using srgamma\_optimize, employing the STORS algorithm.

By default, srgamma\_custom() samples from the standard Gamma distribution with shape = 1 and rate = 1. The proposal distribution is pre-optimized at package load time using srgamma\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

## Value

A numeric vector of length n containing random samples from the Gamma distribution. The shape and rate parameters are specified during the optimization process using srgamma\_optimize().

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

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## Note

This function is not scalable. Therefore, only the srgamma\_custom() version is available, which requires the proposal to be pre-optimized using srgamma\_optimize() before calling this function.

## See Also

srgamma\_optimize to optimize the custom proposal.

## **Examples**

```
# Generate 10 samples from Gamma Distribution
samples <- srgamma_custom(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srgamma_custom(10, x = x)
print(x)</pre>
```

srgamma\_optimize

Optimizing Gamma Distribution proposal

## **Description**

The srgamma\_optimize() function generates an optimized proposal for a targeted Gamma distribution. The proposal can be customized and adjusted based on various options provided by the user.

## Usage

```
srgamma_optimize(
   shape = NULL,
   rate = NULL,
   scale = NULL,
   xl = NULL,
   xr = NULL,
   steps = 4091,
   proposal_range = NULL,
   theta = 0.1,
   target_sample_size = 1000,
   verbose = FALSE
)
```

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## **Arguments**

shape	(optional) Numeric. The shape parameter $(\alpha)$ of the Gamma distribution. Defaults to 1.	
rate	(optional) Numeric. The rate parameter $(\beta)$ of the Gamma distribution. Defaults to 1.	
scale	(optional) Numeric. The scale parameter of the Gamma distribution. Defaults to 1.	
x1	Numeric. Left truncation bound for the target distribution. Defaults to $\emptyset$ , representing no left truncation.	
xr	Numeric. Right truncation bound for the target distribution. Defaults to Inf, representing no right truncation.	
steps	(optional) Integer. Desired number of steps in the proposal. Defaults to 4091.	
proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to NULL, indicating automatic range selection.	
theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.	
target_sample_size		
	(optional) Integer. Target sample size for proposal optimization. Defaults to 1000.	
verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.	

#### **Details**

When srgamma\_optimize() is explicitly called:

- A proposal is created and cached. If no parameters are provided, a standard proposal is created with shape = 1 and rate = 1.
- Providing shape and rate creates a custom proposal, which is cached for use with srgamma\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the target\_sample\_size.

#### Value

A list containing the optimized proposal and related parameters for the specified Gamma distribution. The proposal is also cached for internal use.

data Detailed information about the proposal steps, including x,  $s_{upper}$ ,  $p_a$ , and  $s_{upper}$ lower. areas The areas under the left tail, steps, and right tail of the proposal distribution.

steps\_number The number of steps in the proposal.

f\_params The parameters (shape and rate) of the Gamma distribution.

#### See Also

srgamma\_custom: Function to sample from a custom proposal generated by srgamma\_optimize().

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#### **Examples**

```
# Generate a standard proposal with shape = 1 and rate = 1
standard_proposal <- srgamma_optimize()

# Generate a custom proposal with shape = 2 and rate = 3
custom_proposal <- srgamma_optimize(shape = 2, rate = 3)</pre>
```

srlaplace

Sampling from Laplace Distribution

#### **Description**

The srlaplace() function generates random samples from a Laplace Distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Inverse Transform (IT) method for the tails.

## Usage

```
srlaplace(n = 1, mu = 0, b = 1, x = NULL)
srlaplace\_custom(n = 1, x = NULL)
```

## **Arguments**

n	Integer, length 1. Number of samples to draw.
mu	Numeric, location parameter.
b	Numeric, scale parameter.
x	(optional) Numeric vector of length $n$ . If provided, this vector is over written in place to avoid any memory allocation.

#### **Details**

The Laplace distribution has the probability density function (PDF):  $f(x|\mu,b) = \frac{1}{2b} \exp\left(-\frac{|x-\mu|}{b}\right)$ , where:

 $\mu$  is the location parameter (mean of the distribution).

b is the scale parameter, which controls the spread of the distribution (b > 0).

These two functions are for sampling using the STORS algorithm based on the proposal that has been constructed using srlaplace\_optimize.

By default, srlaplace() samples from a standard Laplace Distribution (mu = 0, b = 1). The proposal distribution is pre-optimized at package load time using srlaplace\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

If srlaplace() is called with custom mu or b parameters, the samples are generated from the standard Laplace Distribution, then scaled and location shifted accordingly.

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#### Value

A numeric vector of length n containing samples from the Laplace Distribution with the specified mu and b.

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

#### See Also

srlaplace\_optimize to optimize the custom or the scaled proposal.

## **Examples**

```
# Generate 10 samples from the standard Laplace Distribution
samples <- srlaplace(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srlaplace(10, x = x)
print(x)

# Generate 10 samples from a Laplace Distribution with mu = 2 and b = 3
samples <- srlaplace(10, mu = 2, b = 3)
print(samples)</pre>
```

srlaplace\_optimize

Optimizing Laplace Distribution proposal

#### **Description**

The srlaplace\_optimize() function generates an optimized proposal for a targeted Laplace Distribution. The proposal can be customized and adjusted based on various options provided by the user.

## Usage

```
srlaplace_optimize(
  mu = NULL,
  b = NULL,
  xl = NULL,
  xr = NULL,
  steps = 4091,
  proposal_range = NULL,
  theta = 0.1,
  target_sample_size = 1000,
  verbose = FALSE,
  symmetric = FALSE
)
```

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## **Arguments**

mu	(optional) Numeric, location parameter.	
b	(optional) Numeric, scale parameter.	
xl	Numeric. Left truncation bound for the target distribution. Defaults to $\neg Inf$ , representing no left truncation.	
xr	Numeric. Right truncation bound for the target distribution. Defaults to ${\tt Inf},$ representing no right truncation.	
steps	(optional) Integer. Desired number of steps in the proposal. Defaults to NULL, which means the number of steps is determined automatically during optimization.	
proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to NULL, indicating automatic range selection.	
theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.	
target_sample_size		
	(optional) Integer. Target sample size for proposal optimization. Defaults to $1000$ .	
verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.	
symmetric	Boolean. If TRUE, the proposal will target only the right tail of the distribution, reducing the size of the cached proposal and making sampling more memory-efficient. An additional uniform random number will be sampled to determine the sample's position relative to the mode of the distribution. While this improves memory efficiency, the extra sampling may slightly impact performance, especially when the proposal efficiency is close to 1. Defaults to FALSE.	

#### **Details**

When srlaplace\_optimize() is explicitly called:

- A proposal is created and cached. If no parameters are provided, a standard proposal is created (mu = 0, b = 1).
- Providing mu or b creates a custom proposal, which is cached for use with srlaplace\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the. target\_sample\_size.

#### Value

The user does not need to store the returned value, because the package internally cashes the proposal. However, we explain here the full returned proposal for advanced users.

A list containing the optimized proposal and related parameters for the specified built-in distribution:

data A data frame with detailed information about the proposal steps, including:

x The start point of each step on the x-axis.

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s\_upper The height of each step on the y-axis.

p\_a Pre-acceptance probability for each step.

s\_upper\_lower A vector used to scale the uniform random number when the sample is accepted.

areas A numeric vector containing the areas under:

left\_tail The left tail bound.

steps The middle steps.

right\_tail The right tail bound.

steps\_number An integer specifying the number of steps in the proposal.

sampling\_probabilities A numeric vector with:

left\_tail The probability of sampling from the left tail.

left\_and\_middle The combined probability of sampling from the left tail and middle steps.

unif\_scaler A numeric scalar, the inverse probability of sampling from the steps part of the proposal  $(\frac{1}{p(lower < x < upper)})$ . Used for scaling uniform random values.

1t\_properties A numeric vector of 5 values required for Adaptive Rejection Sampling (ARS) in the left tail.

rt\_properties A numeric vector of 6 values required for ARS in the right tail.

alpha A numeric scalar representing the uniform step area.

tails\_method A string, either "ARS" (Adaptive Rejection Sampling) or "IT" (Inverse Transform), indicating the sampling method for the tails.

proposal\_bounds A numeric vector specifying the left and right bounds of the target density.

cnum An integer representing the cache number of the created proposal in memory.

symmetric A numeric scalar indicating the symmetry point of the proposal, or NULL if not symmetric.

f\_params A list of parameters for the target density that the proposal is designed for.

mu is the location parameter (location of the distribution).

b is the scale parameter, which controls the spread of the distribution (b > 0).

is\_symmetric A logical value indicating whether the proposal is symmetric.

proposal\_type A string indicating the type of the generated proposal:

"scaled" The proposal is "scalable" and standardized with mu = 0 and b = 1. This is used when parameters mu and b are either NULL or not provided. Scalable proposals are compatible with srlaplace.

"custom" The proposal is "custom" when either mu or b is provided. Custom proposals are compatible with srlaplace\_custom.

target\_function\_area A numeric scalar estimating the area of the target distribution.

dens\_func A string containing the hardcoded density function.

density\_name A string specifying the name of the target density distribution.

lock An identifier used for saving and loading the proposal from disk.

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#### See Also

srlaplace: Function to sample from a scalable proposal generated by srlaplace\_optimize().
srlaplace\_custom: Function to sample from a custom proposal tailored to user specifications.

## **Examples**

```
# Generate scalable proposal that with mu = 0 and b = 1, that has 4096 steps
scalable_proposal <- srlaplace_optimize(steps = 4096)

# Generate custom proposal that with mu = 2 and b = 1
scalable_proposal <- srlaplace_optimize(mu = 2, b = 1)</pre>
```

srnorm

Sampling from Normal Distribution

## Description

The srnorm() function generates random samples from a Normal distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Adaptive Rejection Sampling (ARS) for the tails.

## Usage

```
srnorm(n = 1, mean = 0, sd = 1, x = NULL)
srnorm\_custom(n = 1, x = NULL)
```

## **Arguments**

Integer, length 1. Number of samples to draw.
 Numeric. Mean parameter of the Normal distribution.
 Numeric. Standard deviation of the target Normal distribution.

x (optional) Numeric vector of length n. If provided, this vector is over written in place to avoid any memory allocation.

## Details

The Normal distribution has the probability density function (PDF):  $f(x|\mu,\sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$ , where:

 $\mu$  is the mean of the distribution, which determines the centre of the bell curve.

 $\sigma$  is the standard deviation, which controls the spread of the distribution ( $\sigma > 0$ ).

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These two functions are for sampling using the STORS algorithm based on the proposal that has been constructed using srnorm\_optimize.

By default, srnorm() samples from a standard Normal distribution (mean = 0, sd = 1). The proposal distribution is pre-optimized at package load time using srnorm\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

If srnorm() is called with custom mean or sd parameters, the samples are generated from the standard Normal distribution, then scaled and location shifted accordingly.

#### Value

A numeric vector of length n containing samples from the Normal distribution with the specified mean and sd.

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

#### See Also

srnorm\_optimize to optimize the custom or the scaled proposal.

## **Examples**

```
# Generate 10 samples from the standard Normal distribution
samples <- srnorm(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srnorm(10, x = x)
print(x)

# Generate 10 samples from a Normal distribution with mean = 2 and sd = 3
samples <- srnorm(10, mean = 2, sd = 3)
print(samples)</pre>
```

srnorm\_optimize

Optimizing Normal Distribution proposal

## Description

The srnorm\_optimize() function generates an optimized proposal for a targeted Normal distribution. The proposal can be customized and adjusted based on various options provided by the user.

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## Usage

```
srnorm_optimize(
  mean = NULL,
  sd = NULL,
  xl = -Inf,
  xr = Inf,
  steps = NULL,
  proposal_range = NULL,
  theta = 0.1,
  target_sample_size = 1000,
  verbose = FALSE,
  symmetric = FALSE
)
```

## **Arguments**

mean	(optional) Numeric. Mean parameter of the Normal distribution. Defaults to NULL, which implies a scalable proposal with mean = $0$ .	
sd	(optional) Numeric. Standard deviation of the target Normal distribution. Defaults to NULL, which implies a scalable proposal with sd = 1.	
xl	Numeric. Left truncation bound for the target distribution. Defaults to -Inf, representing no left truncation.	
xr	Numeric. Right truncation bound for the target distribution. Defaults to Inf, representing no right truncation.	
steps	(optional) Integer. Desired number of steps in the proposal. Defaults to NULL, which means the number of steps is determined automatically during optimization.	
proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to NULL, indicating automatic range selection.	
theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.	
target_sample_size		
	(optional) Integer. Target sample size for proposal optimization. Defaults to 1000.	
verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.	
symmetric	Boolean. If TRUE, the proposal will target only the right tail of the distribution, reducing the size of the cached proposal and making sampling more memory-efficient. An additional uniform random number will be sampled to determine the sample's position relative to the mode of the distribution. While this improves memory efficiency, the extra sampling may slightly impact performance, especially when the proposal efficiency is close to 1. Defaults to FALSE.	

## **Details**

When srnorm\_optimize() is explicitly called:

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 A proposal is created and cached. If no parameters are provided, a standard proposal is created (mean = 0, sd = 1).

- Providing mean or sd creates a custom proposal, which is cached for use with srnorm\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the. target\_sample\_size.

#### Value

The user does not need to store the returned value, because the package internally cashes the proposal. However, we explain here the full returned proposal for advanced users.

A list containing the optimized proposal and related parameters for the specified built-in distribution:

data A data frame with detailed information about the proposal steps, including:

x The start point of each step on the x-axis.

s\_upper The height of each step on the y-axis.

p\_a Pre-acceptance probability for each step.

s\_upper\_lower A vector used to scale the uniform random number when the sample is accepted.

areas A numeric vector containing the areas under:

left\_tail The left tail bound.

steps The middle steps.

right\_tail The right tail bound.

steps\_number An integer specifying the number of steps in the proposal.

sampling\_probabilities A numeric vector with:

left\_tail The probability of sampling from the left tail.

left\_and\_middle The combined probability of sampling from the left tail and middle steps.

unif\_scaler A numeric scalar, the inverse probability of sampling from the steps part of the proposal  $(\frac{1}{p(lower < x < upper)})$ . Used for scaling uniform random values.

1t\_properties A numeric vector of 5 values required for Adaptive Rejection Sampling (ARS) in the left tail.

rt\_properties A numeric vector of 6 values required for ARS in the right tail.

alpha A numeric scalar representing the uniform step area.

tails\_method A string, either "ARS" (Adaptive Rejection Sampling) or "IT" (Inverse Transform), indicating the sampling method for the tails.

proposal\_bounds A numeric vector specifying the left and right bounds of the target density.

cnum An integer representing the cache number of the created proposal in memory.

symmetric A numeric scalar indicating the symmetry point of the proposal, or NULL if not symmetric.

f\_params A list of parameters for the target density that the proposal is designed for.

mean The mean of the target distribution.

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sd The standard deviation of the target distribution.

is\_symmetric A logical value indicating whether the proposal is symmetric.

proposal\_type A string indicating the type of the generated proposal:

"scaled" The proposal is "scalable" and standardized with mean = 0 and sd = 1. This is used when parameters mean and sd are either NULL or not provided. Scalable proposals are compatible with srnorm.

"custom" The proposal is "custom" when either mean or sd is provided. Custom proposals are compatible with srnorm\_custom.

target\_function\_area A numeric scalar estimating the area of the target distribution.

dens\_func A string containing the hardcoded density function.

density\_name A string specifying the name of the target density distribution.

lock An identifier used for saving and loading the proposal from disk.

#### See Also

srnorm: Function to sample from a scalable proposal generated by srnorm\_optimize(). srnorm\_custom: Function to sample from a custom proposal tailored to user specifications.

#### **Examples**

```
# Generate scalable proposal that with mean = 0 and sd = 1, that has 4096 steps
scalable_proposal <- srnorm_optimize(steps = 4096)

# Generate custom proposal that with mean = 2 and sd = 1
scalable_proposal <- srnorm_optimize(mean = 2, sd = 1)</pre>
```

srpareto\_custom

Sampling from Pareto Distribution

## Description

The srpareto\_custom() function generates random samples from a Pareto distribution using the STORS algorithm. It employs an optimized proposal distribution around the mode and Inverse Transform (IT) method for the tails.

## Usage

```
srpareto\_custom(n = 1, x = NULL)
```

#### **Arguments**

- n Integer, length 1. Number of samples to draw.
- x (optional) Numeric vector of length n. If provided, this vector is overwritten in place to avoid any memory allocation.

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#### **Details**

The Pareto Distribution

The Pareto distribution has the probability density function (PDF):

$$f(x|\alpha,\sigma) = \frac{\alpha\sigma^{\alpha}}{x^{\alpha+1}}, \quad x \ge \sigma,$$

where:

 $\alpha$  is the shape parameter ( $\alpha > 0$ ), which determines the tail heaviness of the distribution.

 $\sigma$  is the scale parameter ( $\sigma > 0$ ), which determines the minimum possible value of x.

The Pareto distribution is widely used in modelling phenomena with heavy tails, such as wealth distribution, insurance losses, and natural events.

This function samples from a proposal constructed using srpareto\_optimize, employing the STORS algorithm.

By default, srpareto\_custom() samples from the standard Pareto distribution with shape = 1 and rate = 1. The proposal distribution is pre-optimized at package load time using srpareto\_optimize() with steps = 4091, creating a scalable proposal centred around the mode.

#### Value

A numeric vector of length n containing random samples from the Pareto distribution. The shape and scale parameters are specified during the optimization process using srpareto\_optimize().

**NOTE:** When the x parameter is specified, it is updated in-place with the simulation for performance reasons.

#### Note

This function is not scalable. Therefore, only the srpareto\_custom() version is available, which requires the proposal to be pre-optimized using srpareto\_optimize() before calling this function.

## See Also

srpareto\_optimize to optimize the custom proposal.

```
# Generate 10 samples from Pareto Distribution
samples <- srpareto_custom(10)
print(samples)

# Generate 10 samples using a pre-allocated vector
x <- numeric(10)
srpareto_custom(10, x = x)
print(x)</pre>
```

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srpareto\_optimize

Optimizing Pareto Distribution proposal

## Description

The srpareto\_optimize() function generates an optimized proposal for a targeted Pareto Distribution. The proposal can be customized and adjusted based on various options provided by the user.

## Usage

```
srpareto_optimize(
    scale = NULL,
    shape = NULL,
    xl = NULL,
    xr = NULL,
    steps = 4091,
    proposal_range = NULL,
    theta = 0.1,
    target_sample_size = 1000,
    verbose = FALSE
)
```

## Arguments

	scale	(optional) Numeric. scale parameter of the Pareto Distribution. Defaults to NULL, which implies a scalable proposal with scale = 1.
	shape	(optional) Numeric. shape parameter of the Pareto Distribution. Defaults to NULL, which implies a scalable proposal with shape = 1.
	xl	Numeric. Left truncation bound for the target distribution. Defaults to $\neg Inf$ , representing no left truncation.
	xr	Numeric. Right truncation bound for the target distribution. Defaults to Inf, representing no right truncation.
	steps	(optional) Integer. Desired number of steps in the proposal. Defaults to NULL, which means the number of steps is determined automatically during optimization.
	proposal_range	(optional) Numeric vector. Specifies the range for optimizing the steps part of the proposal. Defaults to $NULL$ , indicating automatic range selection.
	theta	Numeric. A parameter for proposal optimization. Defaults to 0.1.
target_sample_size		
		(optional) Integer. Target sample size for proposal optimization. Defaults to $1000$ .
	verbose	Boolean. If TRUE, detailed optimization information, including areas and steps, will be displayed. Defaults to FALSE.

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#### **Details**

When srpareto\_optimize() is explicitly called:

• A proposal is created and cached. If no parameters are provided, a standard proposal is created with rate = 1.

- Providing rate creates a custom proposal, which is cached for use with srpareto\_custom().
- The optimization process can be controlled via parameters such as steps, proposal\_range, or theta. If no parameters are provided, the proposal is optimized via brute force based on the. target\_sample\_size.

#### Value

The user does not need to store the returned value, because the package internally cashes the proposal. However, we explain here the full returned proposal for advanced users.

A list containing the optimized proposal and related parameters for the specified built-in distribution: #'

data Detailed information about the proposal steps, including x, s\_upper, p\_a, and s\_upper\_lower. areas The areas under the left tail, steps, and right tail of the proposal distribution.

steps\_number The number of steps in the proposal.

f\_params The parameters (scale and shape) of the Beta distribution.

#### See Also

srpareto\_custom: Function to sample from a custom proposal tailored to user specifications.

```
# Generate scalable proposal that with rate = 1, that has 4096 steps
scalable_proposal <- srpareto_optimize(steps = 4096)

# Generate custom proposal that with scale = 4
scalable_proposal <- srpareto_optimize(scale = 4)</pre>
```

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