

# Package ‘DCL’

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**Title** Claims Reserving under the Double Chain Ladder Model

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**Description** Statistical modelling and forecasting in claims reserving in non-life insurance under the Double Chain Ladder framework by Martinez-Miranda, Nielsen and Verrall (2012).

**License** GPL-2

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DCL-package

*Claims Reserving under the Double Chain Ladder Model*

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## Description

This package provides functions for statistical modelling and forecasting in claims reserving in non-life insurance under the Double Chain Ladder framework by Martinez-Miranda, Nielsen and Verrall (2012). Using specific functions, the user will be able generate plots to visualize and gain intuition about the data (run-off triangles), break down classical chain ladder under the DCL model, visualize the underlying delay function and the inflation, introduce expert knowledge about the severity inflation, the zero-claims etc. Besides a validation exercise can be performed through a back-test on the data.

## Details

Package: DCL  
 Type: Package  
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 License: GPL-2

## Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

Maintainer: Maria Dolores Martinez-Miranda <mmiranda@ugr.es>

## References

Martinez-Miranda M.D., Nielsen B, Nielsen J.P and Verrall, R. (2011) Cash flow simulation for a model of outstanding liabilities based on claim amounts and claim numbers. *Astin Bulletin*, 41/1,

107-129.

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

See more at <http://www.cassknowledge.com/research/article/double-chain-ladder-cass-knowledge>

## Examples

```
data(NtriangleDCL)
data(XtriangleDCL)

# Classical chain ladder parameters
my.clm.par<-clm(XtriangleDCL)
Plot.clm.par(my.clm.par)

# Estimation of the DCL parameters (break-down of the chain ladder parameters)
my.dcl.par<-dcl.estimation(XtriangleDCL,NtriangleDCL)
Plot.dcl.par(my.dcl.par)

# DCL Predictions by diagonals (future calendar years)
# Splitting the chain ladder reserve into RBNR and IBNR claims (ignoring the tail)
preds.dcl.diag<-dcl.predict(my.dcl.par,Model=0,Tail=FALSE,num.dec=0)

# Full cashflow considering the tail (only the variance process)
# Below only B=200 simulations for faster calculations in the example
boot1<-dcl.boot(dcl.par=my.dcl.par,Ntriangle=NtriangleDCL,boot.type=1,B=200)
Plot.cashflow(boot1)
```

---

Aggregate

*Switch to a higher level of aggregation*

---

## Description

From the input run-off triangle (weekly, monthly, quarterly, etc.) the function creates another triangle on a higher level of aggregation.

## Usage

```
Aggregate(triangle, freq = 4)
```

**Arguments**

triangle	The original run-off (incremental) triangle. It should be a squared matrix (let denote by $m$ its dimension $m$ ).
freq	The frequency to be considered in the aggregation. The default value is 4, to be used to construct a yearly run-off triangle from a quarterly triangle.

**Details**

If the input triangle does not consist of complete periods (for example a quarterly triangle with only three quarters in the last year), then the last (lower level) periods will be removed to get full aggregated periods.

**Value**

A run-off triangle in the specified higher level of aggregation.

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**See Also**

[get.incremental](#), [get.cumulative](#), [Plot.triangle](#)

**Examples**

```
## A dummy example: a run-off triangle with 5*4=20 quarters
m<-20
my.square<-matrix(1,m,m)
# Now my.triangle is a quarterly triangle (the upper left triangle from my.square)
my.triangle<-my.square
my.triangle[row(my.square)+col(my.square)>(m+1)]<-NA
my.yearly.triangle<-Aggregate(my.triangle)
list(original=my.triangle,yearly=my.yearly.triangle)
```

---

 bdcl. estimation

---

*Parameter estimation - DCL model using the BDCL method*


---

**Description**

Estimate the parameters in the Double Chain Ladder model (delay parameters, severity mean and variance) using the Double Chain Ladder method with a Bornhuetter-Ferguson adjustment. The Bornhuetter-Ferguson technique is applied to stabilise the underwriting inflation parameters using incurred data

**Usage**

```
bdcl. estimation( Xtriangle , Ntriangle , Itriangle , adj = 1 ,
  Tables=TRUE , num. dec=4 , n. cal=NA , Fj. X=NA , Fj. N=NA , Fj. I=NA)
```

**Arguments**

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years, etc.))
Itriangle	The incurred triangle. It should be a matrix with incurred data located in the upper triangle. It is an incremental run-off triangle with the same dimension as Xtriangle (both in the same aggregation level (quarters, years, etc.))
adj	Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See more in details below.
Tables	Logical. If TRUE (default) it is showed a table with the estimated parameters.
num. dec	Number of decimal places used to report numbers in the tables (if Tables=TRUE).
n. cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n. cal=NA and all the observed calendars are used (classical chain ladder).
Fj. X	Optional vector with length m-1 (m being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from Xtriangle. See more details in <a href="#">clm</a> .
Fj. N	Optional vector with length m-1 with the development factors to calculate the chain ladder estimates from Ntriangle.
Fj. I	Optional vector with length m-1 with the development factors to calculate the chain ladder estimates from Itriangle.

**Details**

Two model are estimated in the double chain ladder framework as with the `dcl. estimation` function. In this case the inflation parameter (`inflat`) is estimated from the incurred triangle (see BF adjustment in the description of the BDCL method in Martinez-Miranda, Nielsen and Verrall 2013). The predicted reserve using these estimates is different from the incurred reserve. If you want to reproduce exactly the incurred reserve (by splitting it into its RBNS and IBNR components) then use the function `idcl. estimation`.

**Value**

<code>pi. delay</code>	General delay parameters
<code>mu</code>	Mean severity factor
<code>inflat</code>	Underwriting severity inflation (BDCL inflation)

inflatt.DCL	Underwriting severity inflation (DCL inflation)
pj	Delay probabilities (under a Multinomial assumption)
mu.adj	Adjusted mean factor corresponding to the pj parameters
sigma2	Variance severity factor
phi	Overdispersion parameter used to derive the estimate sigma2
Ey	Severity mean for each underwriting period
Vy	Severity variance for each underwriting period
adj	Type of adjusted used to derive the pj probabilities
alpha.N	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle (Ntriangle)
beta.N	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle (Ntriangle)
Nhat	The chain ladder predictions (counts triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
alpha.X	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle (Xtriangle)
beta.X	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle (Xtriangle)
Xhat	The chain ladder predictions (paid triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
alpha.I	Underwriting chain ladder parameter in the (OD)-Poisson model. Incurred triangle (Itriangle)
beta.I	Underwriting chain ladder parameter in the (OD)-Poisson model. Incurred triangle (Itriangle)

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

### References

- Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.
- Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*.

### See Also

[get.incremental](#), [Plot.dcl.par](#), [dcl.predict](#), [dcl. estimation](#), [idcl. estimation](#), [clm](#)

## Examples

```
# Reproducing the data analysis in the paper by Martinez-Miranda, Nielsen and Verrall (2013)
data(NtriangleBDCL)
data(XtriangleBDCL)
data(ItriangleBDCL)

my.bdcl.par<-bdcl. estimation(XtriangleBDCL,NtriangleBDCL,ItriangleBDCL)
# Parameters shown in Table 1
Plot.dcl.par(my.bdcl.par,type.inflat='BDCL')
# BDCL Predictions by diagonals (future calendar years)
preds.bdcl.diag<-dcl.predict(my.bdcl.par,NtriangleBDCL,num.dec=0)
```

---

clm

*Classical Chain Ladder Method*


---

## Description

Provide the classical chain ladder output consisting of the development (forward) factors and the predictions in the full square. Besides it provides the estimated parameters under the (over-dispersion) Poisson model for the double chain ladder estimation.

## Usage

```
clm( triangle , n.cal = NA , Fj = NA )
```

## Arguments

triangle	The loss triangle. It should be a matrix with the observed counts (number of reported claims, number of payments etc.), aggregated payments or incurred data, located in the upper triangle. The lower triangle should consist of missing (NA) or zero values.
n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).
Fj	Optional. A vector with length m-1 (m being the dimension of the triangle) with the development factors to calculate the chain ladder estimates. See more details below.

## Details

By default Fj=NA and then classical chain ladder with the common calculation of the development factors (or using the most recent calendars -if  $0 < n.cal < m$  is provided), is performed. By specifying a valid vector with the development factors (it should has length equal to m-1), the user is allowed to use his own values in the algorithm. If valid values are specified for both n.cal and Fj, the first one (n.cal) will be ignored and the given development factors will be used in the calculations.

**Value**

triangle.hat	A matrix with dimension $m$ having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
alpha	Underwriting chain ladder parameter in the (OD)-Poisson model (see for example Verrall (1991) for a formal definition)
beta	Underwriting chain ladder parameter in the (OD)-Poisson model (Verrall 1991)
Fj	Development (forward) factors

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

- Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.
- Verrall, R. (1991) Chain ladder and Maximum Likelihood. *Journal of the Institute of Actuaries* 118, 489-499.

**See Also**

[get.incremental](#), [Plot.clm.par](#), [Plot.triangle](#)

**Examples**

```
data(NtriangleDCL)
clm.N<-clm(NtriangleDCL)
# The alpha's
clm.N$alpha
# The beta's
clm.N$beta
# The development factors
clm.N$Fj
# Plotting the parameters and the dev. factors
Plot.clm.par(clm.N)
# The predictions
Nhat<-clm.N$triangle.hat
Plot.triangle(Nhat,Histogram=TRUE)

## Trying variations from classical chain ladder
# Try CLM only using the more recent 2 calendars in the development
# factors calculation
clm(NtriangleDCL,n.cal=2)

# Try CLM providing a vector with given development factors
my.Fj<-c(1.4,1.1,1.0,1.1,1.1,1.0,1.0,1.0,1.1)
clm(NtriangleDCL,Fj=my.Fj)
```



---

dcl.boot	<i>Bootstrap distribution: the full cashflow</i>
----------	--

---

### Description

Provide the distribution of the IBNR, RBNS and total (RBNS+IBRN) reserves by calendar years and rows using bootstrapping.

### Usage

```
dcl.boot( dcl.par , sigma2 , Ntriangle , boot.type = 2 , B = 999 ,
  Tail = TRUE , summ.by = "diag" , Tables = TRUE , num.dec = 2 , n.cal = NA)
```

### Arguments

dcl.par	A list object with the estimated parameters: the value returned by the functions <a href="#">dcl. estimation</a> , <a href="#">bdcl. estimation</a> or <a href="#">idcl. estimation</a> .
sigma2	Optional. The variance of the individual payments in the first underwriting period.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should be the same triangle used to get the value passed by the argument dcl.par.
boot.type	Choose between values 1, to provide only the variance process, or 2 (default), to take into account the uncertainty of the parameters.
B	The number of simulations in the bootstrap algorithm. The default value is 999.
Tail	Logical. If TRUE (default) the tail is provided.
summ.by	A character value such as "diag", "row" or "cell".
Tables	Logical. If TRUE (default) it is showed a table with the summary (mean, standard deviation, 1%, 5%, 50%, 95%, 99%) of the distribution of the outstanding liabilities in the future calendar periods (if summ.by="diag") or by underwriting period (if summ.by="row").
num.dec	Number of decimal places used to report numbers in the tables. Used only if Tables=TRUE
n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).

### Details

If the calculated severity variance using the function [dcl. estimation](#) is not a valid estimate then it is recommended to provide directly this value through the argument `sigma2`. It can be calculated using the function `var` applied to a pilot sample of individual payments observed in the first underwriting period.

**Value**

<code>array.rbns.boot</code>	An array with dimensions $(m, 2m-1, B)$ ( $m$ being the dimension of the input triangles in DCL). Each <code>array.rbns.boot[, , b]</code> is a matrix, with $m$ rows and $2m-1$ columns, having the bootstrapped outstanding RBNS numbers as the entries (for $b=1, \dots, B$ ).
<code>Mat.rbns</code>	A matrix with $B$ rows and $2m$ columns. Each <code>Mat.rbns[b, ]</code> is a vector with elements being the outstanding liabilities for RBNS claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).
<code>array.ibnr.boot</code>	An array with dimensions $(m, 2m-1, B)$ ( $m$ being the dimension of the input triangles in DCL). Each <code>array.ibnr.boot[, , b]</code> is a matrix, with $m$ rows and $2m-1$ columns, having the bootstrapped outstanding IBNR numbers as the entries (for $b=1, \dots, B$ ).
<code>Mat.ibnr</code>	A matrix with $B$ rows and $2m$ columns. Each <code>Mat.ibnr[b, ]</code> is a vector with elements being the outstanding liabilities for IBNR claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).
<code>Mat.total</code>	A matrix with $B$ rows and $2m$ columns. Each <code>Mat.total[b, ]</code> is a vector with elements being the outstanding liabilities for total(=RBNS+IBNR) claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).
<code>summ.rbns</code>	A dataframe with the summary of the RBNS distribution. Only if <code>Tables=TRUE</code> .
<code>summ.ibnr</code>	A dataframe with the summary of the IBNR distribution. Only if <code>Tables=TRUE</code> .
<code>summ.total</code>	A dataframe with the summary of the total(=RBNS+IBNR) distribution. Only if <code>Tables=TRUE</code> .

**Note**

If `boot.type=2` the function will take some time to perform the calculations. It increases with the dimension of the triangles and the specified number of simulations  $B$ .

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*.

**See Also**

[Plot.cashflow](#), [dcl.boot.prior](#)

## Examples

```
# Results described in the data application by Martinez-Miranda, Nielsen and Verrall (2012)
data(NtriangleDCL)
data(XtriangleDCL)

# Estimation of the DCL parameters
est<-dcl.estimation(XtriangleDCL,NtriangleDCL)

# Full cashflow considering the tail (only the variance process)
# Below only B=200 simulations to be faster in the example
boot1<-dcl.boot(dcl.par=est,Ntriangle=NtriangleDCL,boot.type=1,B=200)
Plot.cashflow(boot1)

# Full cashflow with tail and taking into account the parameters uncertainty
# and B=999 simulations. Do not run it unless you can wait about one minute
# boot2<-dcl.boot(dcl.par=est,Ntriangle=NtriangleDCL,boot.type=2)
# Plot.cashflow(boot2)
```

---

dcl.boot.prior	<i>Bootstrap distribution (the full cashflow) adding prior knowledge</i>
----------------	--

---

## Description

Provide the distribution of the IBNR, RBNS and total (RBNS+IBRN) reserves by calendar years and rows using bootstrapping.

## Usage

```
dcl.boot.prior( Xtriangle , Ntriangle , sigma2 , mu , inflat.i , inflat.j , Qi ,
  Model = 2 , adj = 1 , boot.type = 2, B = 999 ,
  Tail = TRUE , summ.by = "diag", Tables = TRUE, num.dec = 2 , n.cal = NA ,
  Fj.X = NA , Fj.N = NA )
```

## Arguments

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
sigma2	Optional. The variance of the individual payments in the first underwriting period.
mu	Optional. The mean of the individual payments in the first underwriting period.
inflat.i	Optional. A vector with dimension m (the dimension of the input triangles) specifying the severity inflation in the underwriting direction.

<code>inflat.j</code>	Optional. A vector with dimension $m$ specifying the severity inflation in the development direction. If not specified it will be assumed to be 1 and then the severity mean not depending on the development period.
<code>Qi</code>	Optional. A vector with dimension $m$ specifying the probability of zero-claims for each underwriting period. If not specified then it will be assumed no zero-payments.
<code>Model</code>	Possible values are 0, 1 or 2 (default). See <a href="#">dcl. estimation</a> for more in details.
<code>adj</code>	Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See <a href="#">dcl. estimation</a> for more details.
<code>boot.type</code>	Choose between values 1, to provide only the variance process, or 2 (default), to take into account the uncertainty of the parameters.
<code>B</code>	The number of simulations in the bootstrap algorithm. The default value is 999.
<code>Tail</code>	Logical. If TRUE (default) the tail is provided.
<code>summ.by</code>	A character value such as "diag", "row" or "cell".
<code>Tables</code>	Logical. If TRUE (default) it is showed a table with the summary (mean, standard deviation, 1%, 5%, 50%, 95%, 99%) of the distribution of the outstanding liabilities in the future calendar periods (if <code>summ.by="diag"</code> ) or by underwriting period (if <code>summ.by="row"</code> ).
<code>num.dec</code>	Number of decimal places used to report numbers in the tables. Used only if <code>Tables=TRUE</code>
<code>n.cal</code>	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default <code>n.cal=NA</code> and all the observed calendars are used (classical chain ladder).
<code>Fj.X</code>	Optional vector with length $m-1$ ( $m$ being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from <code>Xtriangle</code> . See more details in <a href="#">clm</a> .
<code>Fj.N</code>	Optional vector with length $m-1$ with the development factors to calculate the chain ladder estimates from <code>Ntriangle</code> .

### Details

If proper values are provided for the arguments `sigma2`, `mu`, `inflat.i`, `inflat.j` and `Qi` then, they will be considered fixed as prior knowledge. Otherwise, if not specified, `inflat.j` will be assumed to be a vector of ones, `Qi` a vector of zeros, and the rest will be estimated using [dcl. estimation](#).

### Value

`array.rbns.boot`

An array with dimensions  $(m, 2m-1, B)$  ( $m$  being the dimension of the input triangles in DCL). Each `array.rbns.boot[, , b]` is a matrix, with  $m$  rows and  $2m-1$  columns, having the bootstrapped outstanding RBNS numbers as the entries (for  $b=1, \dots, B$ ).

`Mat.rbns`

A matrix with  $B$  rows and  $2m$  columns. Each `Mat.rbns[b, ]` is a vector with elements being the outstanding liabilities for RBNS claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).

array.ibnr.boot	An array with dimensions (m,2m-1,B) (m being the dimension of the input triangles in DCL). Each array.ibnr.boot[, ,b] is a matrix, with m rows and 2m-1 columns, having the bootstrapped outstanding IBNR numbers as the entries (for b=1,...,B).
Mat.ibnr	A matrix with B rows and 2m columns. Each Mat.ibnr[b, ] is a vector with elements being the outstanding liabilities for IBNR claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).
Mat.total	A matrix with B rows and 2m columns. Each Mat.total[b, ] is a vector with elements being the outstanding liabilities for total(=RBNS+IBNR) claims in the future calendar periods (sums by diagonals), and last value is the RBNS reserve (overall sum).
summ.rbns	A dataframe with the summary of the RBNS distribution. Only if Tables=TRUE.
summ.ibnr	A dataframe with the summary of the IBNR distribution. Only if Tables=TRUE.
summ.total	A dataframe with the summary of the total(=RBNS+IBNR) distribution. Only if Tables=TRUE.

**Note**

If boot.type=2 the function will take some time to perform the calculations. It increases with the dimension of the triangles and the specified number of simulations B.

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

**See Also**

[Plot.cashflow](#), [dcl.boot](#)

**Examples**

```
## Data application by in Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013)
data(NtrianglePrior)
data(NpaidPrior)
data(XtrianglePrior)

## Extract information about zero-claims and severity dev. inflation
my.priors<-extract.prior(XtrianglePrior,NpaidPrior,NtrianglePrior,Plots=FALSE)
my.inflat.j<-my.priors$inflat.j
my.Qi<-my.priors$Qi

## Bootstrap cashflow incorporating prior knowledge about
##      severity inflation and zero claims
```

```

# Only variance process
# Below only B=200 simulations for a fast example
dist.priorC.I<-dcl.boot.prior(NtrianglePrior,XtrianglePrior,
  inflat.j=my.inflat.j,Qi=my.Qi,adj=2,Tail=FALSE,boot.type=1,B=200)
Plot.cashflow(dist.priorC.I)

## Try to compare with DCL with no prior knowledge:
# Only variance process
# dist.dcl.I<-dcl.boot.prior(NtrianglePrior,XtrianglePrior,adj=2,
#   Tail=FALSE,boot.type=1)
# Plot.cashflow(dist.dcl.I)

```

---

dcl.estimation                      *Parameter estimation - Double Chain Ladder model*

---

## Description

Compute the estimated parameters in the model (delay parameters, severity underwriting inflation, severity mean and variance) using the Double Chain Ladder method.

## Usage

```

dcl.estimation( Xtriangle , Ntriangle , adj = 1 , Tables = TRUE ,
  num.dec = 4 , n.cal = NA , Fj.X=NA , Fj.N=NA )

```

## Arguments

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
adj	Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See more in details below.
Tables	Logical. If TRUE (default) it is showed a table with the estimated parameters.
num.dec	Number of decimal places used to report numbers in the tables (if Tables=TRUE).
n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).
Fj.X	Optional vector with length m-1 (m being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from Xtriangle. See more details in <a href="#">clm</a> .
Fj.N	Optional vector with length m-1 with the development factors to calculate the chain ladder estimates from Ntriangle.

## Details

Two models are estimated in the double chain ladder framework (Martinez-Miranda, Nielsen and Verrall 2012).

The basic DCL model only makes assumption on the first moments (see assumptions M1-M3 in Section 2 of the paper). From the two input triangles ( $N_{triangle}$ ,  $X_{triangle}$ ) the parameters involved in this model are estimated:  $\pi$ .delay (delay parameters that could be negative values and/or sum up above 1, by solving the linear system (7) in Section 3),  $\mu$  (mean of the individual payments in the first underwriting period, from expression (9)),  $inflat$  (the underwriting severity mean inflation, from expression (8)),  $\alpha.N$  and  $\beta.N$  (the chain ladder parameters in the (OD)Poisson model for  $N_{triangle}$  from expressions (10)-(12)). Using the estimated parameters in this simpler model the predicted outstanding numbers (calculated from equations (14) and (15)) are exactly the classical chain ladder predictions (see Theorem 1 in pp. 67).

The second model is a distributional model (assumptions D1-D4 in Section 5) which allows to provide the full cash-flow. In this model the parameters are adjusted to match with the assumptions:  $p_j$  are delay probabilities resulting from adjusting the general parameters  $\pi$ .delay (defined in expressions (21)-(22)),  $\mu$ .adj is the corresponding adjusted mean factor and  $\sigma^2$  is the variance factor (in expression (24)). The function `dcl. estimation` suggest two different adjustments of the general  $\pi$ .delay, the user should choose the adjustment which does not modify substantially the IBNR/RBNS split in the basic model (M1-M3), see Martinez-Miranda, Nielsen, Verrall and Wlthrich (2013) for a discussion.

## Value

$\pi$ .delay	General delay parameters
$\mu$	Mean severity factor
$inflat$	Underwriting severity inflation
$p_j$	Delay probabilities (under a Multinomial assumption)
$\mu$ .adj	Adjusted mean factor corresponding to the $p_j$ parameters
$\sigma^2$	Variance severity factor
$\phi$	Overdispersion parameter used to derive the estimate $\sigma^2$
$E_y$	Severity mean for each underwriting period
$V_y$	Severity variance for each underwriting period
adj	Type of adjusted used to derive the $p_j$ probabilities
$\alpha.N$	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle ( $N_{triangle}$ )
$\beta.N$	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle ( $N_{triangle}$ )
$N_{hat}$	The chain ladder predictions (counts triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
$\alpha.X$	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle ( $X_{triangle}$ )
$\beta.X$	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle ( $X_{triangle}$ )

Xhat                    The chain ladder predictions (paid triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

### References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wlthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*.

### See Also

[Plot.dcl.par](#), [dcl.predict](#), [bdcl.estimation](#), [idcl.estimation](#), [clm](#)

### Examples

```
data(NtriangleDCL)
data(XtriangleDCL)
# Estimation of the DCL parameters described in Martinez-Miranda, Nielsen and Verrall (2012)
est1<-dcl.estimation(XtriangleDCL,NtriangleDCL)
Plot.dcl.par(est1)
# Compare two possible adjustmets to get distributional parameters
# est1 with adj=1
pj.1<-est1$pj
pi.delay<-est1$pi.delay
est2<-dcl.estimation(XtriangleDCL,NtriangleDCL,adj=2,Tables=FALSE)
pj.2<-est2$pj
data.frame(pi.delay=pi.delay,pj.adj.1=pj.1,pj.adj.2=pj.2)
```

---

dcl.predict

*Pointwise predictions (RBNS/IBNR split)*

---

### Description

Pointwise predictions by calendar years and rows of the outstanding liabilities. The predictions are splitted between RBNS and IBNR claims.

### Usage

```
dcl.predict( dcl.par , Ntriangle , Model = 2 , Tail = TRUE ,
  Tables = TRUE , summ.by="diag", num.dec = 2 )
```



**Arguments**

dcl.par	A list object with the estimated parameters: the value returned by the functions <code>dcl. estimation</code> , <code>bdcl. estimation</code> or <code>idcl. estimation</code> .
Ntriangle	Optional. The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should have the same dimension as the Xtriangle (both in the same aggregation level (quarters, years, etc.)) used to derive <code>dcl.par</code>
Model	Possible values are 0, 1 or 2 (default). See more details below.
Tail	Logical. If TRUE (default) the tail is provided.
Tables	Logical. If TRUE (default) it is shown a table with the predicted outstanding liabilities in the future calendar periods ( <code>summ.by="diag"</code> ) or by underwriting period ( <code>summ.by="row"</code> ).
summ.by	A character value such as <code>"diag"</code> , <code>"row"</code> or <code>"cell"</code> .
num.dec	Number of decimal places used to report numbers in the tables. Used only if <code>Tables=TRUE</code>

**Details**

If `Model=0` or `Model=1` then the predictions are calculated using the DCL model parameters in assumptions M1-M3 (general delay parameters, see Martinez-Miranda, Nielsen and Verrall 2012). If `Model=2` the adjusted delay probabilities (distributional model D1-D4) are considered. By choosing `Model=0` the predictions are calculated ignoring the observed counts in `Ntriangle` (also if the `Ntriangle` is not specified). It should be specified to reproduce get the IBNR/RBNS split of classical paid chain ladder.

Choose `summ.by="diag"` to calculate the predicted outstanding liabilities in the future calendar periods (diagonal sums), `summ.by="row"` for sums by underwriting periods (row sums); or `summ.by="cell"` to get only the the individual cell predictions.

**Value**

Xrbns	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding RBNS numbers as the entries.
Drbns	A vector with dimension $2m-1$ with elements being the outstanding liabilities for RBNS claims in the future calendar periods (sums by diagonals). The last value is the RBNS reserve (overall sum).
Rrbns	A vector with dimension $m$ with elements being the outstanding liabilities for RBNS claims at each underwriting period (sums by rows). The last value is the RBNS reserve (overall sum).
Xibnr	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding IBNR numbers as the entries.
Dibnr	A vector with dimension $2m-1$ with elements being the outstanding liabilities for IBNR claims in the future calendar periods (sums by diagonals). The last value is the IBNR reserve (overall sum).

Ribnr	A vector with dimension $m$ with elements being the outstanding liabilities for IBNR claims at each underwriting period (sums by rows). The last value is the RBNS reserve (overall sum).
Xtotal	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding total (=RBNS+IBNR) numbers as the entries.
Dtotal	A vector with dimension $2m-1$ with elements being the outstanding liabilities for all claims in the future calendar periods (sums by diagonals). The last value is the total (=RBNS+IBNR) reserve (overall sum).
Rtotal	A vector with dimension $m$ with elements being the outstanding liabilities for all claims at each underwriting period (sums by rows). The last value is the total (=RBNS+IBNR) reserve (overall sum).

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

### References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wlthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*.

### See Also

[dcl. estimation](#), [bdcl. estimation](#), [idcl. estimation](#), [dcl. predict. prior](#)

### Examples

```
## Data application by in Martinez-Miranda, Nielsen and Verrall (2012)

data(NtriangleDCL)
data(XtriangleDCL)

# Estimation of the DCL parameters described
est<-dcl. estimation(XtriangleDCL,NtriangleDCL)

# with general delay parameters and ignoring Ntriangle to reproduce exactly chain ladder
pred1<-dcl. predict(dcl. par=est,Model=1,Tail=FALSE)

# with Modeled parameters (distributional Model) and ignoring Ntriangle
pred2<-dcl. predict(dcl. par=est,Model=2,Tail=FALSE)

# with Modeled parameters (distributional Model) using observed Ntriangle
pred3<-dcl. predict(dcl. par=est,Ntriangle=NtriangleDCL,Model=2,Tail=FALSE)

# providing the Tail, with Modeled parameters (distributional Model)
pred4<-dcl. predict(dcl. par=est,Ntriangle=NtriangleDCL,Model=2,Tail=TRUE)
```

---

dcl.predict.prior      *Pointwise predictions (RBNS/IBNR split) adding prior knowledge*

---

## Description

Pointwise predictions by calendar years and rows of the outstanding liabilities. The predictions are splitted between RBNS and IBNR claims.

## Usage

```
dcl.predict.prior( Ntriangle , Xtriangle , inflat.i , inflat.j , Qi ,
  Model = 2, adj = 2, Tail = FALSE, Tables = TRUE,
  summ.by = "diag", num.dec = 2 )
```

## Arguments

Ntriangle	Optional. The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as the Xtriangle (both in the same aggregation level (quarters, years,etc.)) used to derive dcl.par
Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
inflat.i	Optional. A vector with dimension m (the dimension of the input triangles) specifying the severity inflation in the underwriting direction. If not specified it will be estimated using <a href="#">dcl. estimation</a> .
inflat.j	Optional. A vector with dimension m specifying the severity inflation in the development direction. If not specified it will be assumed to be 1 and then the severity mean not depending on the development period.
Qi	Optional. A vector with dimension m specifying the probability of zero-claims for each underwriting period. If not specified then it will be assumed no zero-payments.
Model	Possible values are 0, 1 or 2 (default). See <a href="#">dcl. estimation</a> for more in details.
adj	Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See <a href="#">dcl. estimation</a> for more in details.
Tail	Logical. If TRUE (default) the tail is provided.
Tables	Logical. If TRUE (default) it is showed a table with the predicted outstanding liabilities in the future calendar periods (summ.by="diag") or by underwriting period (summ.by="row").
summ.by	A character value such as "diag", "row" or "cell".
num.dec	Number of decimal places used to report numbers in the tables. Used only if Tables=TRUE

### Details

The predictions are calculated under the first moment assumptions in the DCL model (see M1-M3) in Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012). In this case the severity mean is specified as

$$\text{inflat.i} * (1 - Q_i) * \text{inflat.j} * \mu$$

where `inflat.i`, `Qi`, `inflat.j` and `mu` are prior information specified by the user. With this specification, the prediction formula consists of the expectation (conditional expectation -if `Ntriangle` is given and `Model=0`) of the future (RBNS/IBNR) aggregated payments. See formulas (8)-(9) in the paper.

If the prior information is not provided the function will return the DCL predictions as `dcl.predict`. The information about `Qi`, `inflat.j` can be extracted through DCL using `extract.prior`.

### Value

<code>Xrbns</code>	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding RBNS numbers as the entries.
<code>Drbns</code>	A vector with dimension $2m-1$ with elements being the outstanding liabilities for RBNS claims in the future calendar periods (sums by diagonals). The last value is the RBNS reserve (overall sum).
<code>Rrbns</code>	A vector with dimension $m$ with elements being the outstanding liabilities for RBNS claims at each underwriting period (sums by rows). The last value is the RBNS reserve (overall sum).
<code>Xibnr</code>	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding IBNR numbers as the entries.
<code>Dibnr</code>	A vector with dimension $2m-1$ with elements being the outstanding liabilities for IBNR claims in the future calendar periods (sums by diagonals). The last value is the IBNR reserve (overall sum).
<code>Ribnr</code>	A vector with dimension $m$ with elements being the outstanding liabilities for IBNR claims at each underwriting period (sums by rows). The last value is the RBNS reserve (overall sum).
<code>Xtotal</code>	A matrix with dimension $m$ by $2m-1$ ( $m$ being the dimension of the input triangles in DCL) having the outstanding total (=RBNS+IBNR) numbers as the entries.
<code>Dtotal</code>	A vector with dimension $2m-1$ with elements being the outstanding liabilities for all claims in the future calendar periods (sums by diagonals). The last value is the total (=RBNS+IBNR) reserve (overall sum).
<code>Rtotal</code>	A vector with dimension $m$ with elements being the outstanding liabilities for all claims at each underwriting period (sums by rows). The last value is the total (=RBNS+IBNR) reserve (overall sum).

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

## References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

## See Also

[dcl. estimation](#), [bdcl. estimation](#), [idcl. estimation](#), [dcl. predict, extract. prior](#)

## Examples

```
## Data application by in Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013)
data(NtrianglePrior)
data(NpaidPrior)
data(XtrianglePrior)

Ntriangle<-NtrianglePrior
Xtriangle<-XtrianglePrior
Npaid<-NpaidPrior

## Extract information about zero-claims and severity dev. inflation
my.priors<-extract.prior(Xtriangle,Npaid,Ntriangle)
my.inflat.j<-my.priors$inflat.j
my.Qi<-my.priors$Qi

# Reproducing the poinwise predicions (tables 3,4,5) in the paper
# Note: in the paper we did not use Ntriangle in the predictions
# when modelling the predictions are slightly different

## Prior A: only using development year inflation
m<-nrow(Ntriangle)
preds.prior.A.gen<-dcl.predict.prior(Ntriangle,Xtriangle,
  inflat.j=my.inflat.j,Qi=rep(0,m),Model=0,adj=1,
  Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

preds.prior.A.mod<-dcl.predict.prior(Ntriangle,Xtriangle,
  inflat.j=my.inflat.j,Qi=rep(0,m),Model=2,adj=2,
  Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

## Prior B: only using zero claims inflation
preds.prior.B.gen<-dcl.predict.prior(Ntriangle,Xtriangle,
  inflat.j=rep(1,m),Qi=my.Qi,Model=0,adj=1,
  Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

preds.prior.B.mod<-dcl.predict.prior(Ntriangle,Xtriangle,
  inflat.j=rep(1,m),Qi=my.Qi,Model=2,adj=2,
  Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

## Prior C: only using development inflation and zero claims inflation
preds.prior.C.gen<-dcl.predict.prior(Ntriangle,Xtriangle,
```

```

inflat.j=my.inflat.j,Qi=my.Qi,Model=0,adj=1,
Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

preds.prior.C.mod<-dcl.predict.prior(Ntriangle,Xtriangle,
inflat.j=my.inflat.j,Qi=my.Qi,Model=2,adj=2,
Tail=FALSE,Tables=TRUE,summ.by="diag",num.dec=2)

```

---

extract.prior

*Extracting information about zero-claims and severity inflation*


---

## Description

A way of extracting information about zero-claims and severity development inflation through the DCL method applied to two counts triangles: number of payments and number of reported claims.

## Usage

```

extract.prior(Xtriangle, Npaid, Ntriangle, Plots = TRUE , n.cal = NA ,
Fj.X = NA , Fj.N = NA , Fj.Npaid = NA )

```

## Arguments

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Npaid	A run-off (incremental) triangle with the number of payments. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
Plots	Logical. If TRUE (default) it is showed a two by one plot showing the extracted severity inflation in the development direction and the probability of zero-claims for each underwriting period.
n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).
Fj.X	Optional vector with lentgth m-1 (m being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from Xtriangle. See more details in <a href="#">c1m</a> .
Fj.Npaid	Optional vector with lentgth m-1 with the development factors to calculate the chain ladder estimates from Npaid.
Fj.N	Optional vector with lentgth m-1 with the development factors to calculate the chain ladder estimates from Ntriangle.

**Details**

The function implements the strategy proposed in the paper by Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013) to extract information for additional triangles (see "Section 5: An example showing how other data can be used to provide prior information in practice"). The derived severity inflation `inflat.j` does not extend to the tail. If you want provide the tail, by using [dcl.predict.prior](#), the vector should be extended to have dimension  $2m-1$ , otherwise the tail will be not provided (as was done in the cited paper).

**Value**

<code>inflat.j</code>	A vector with dimension $m$ with the extracted severity inflation in the development direction.
<code>Qi</code>	A vector with dimension $m$ with the extracted probability of zero-claims for underwriting period.

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

**See Also**

[dcl.predict.prior](#), [dcl. estimation](#)

**Examples**

```
## Data application in Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013)
data(NtrianglePrior)
data(NpaidPrior)
data(XtrianglePrior)

extract.prior(XtrianglePrior,NpaidPrior,NtrianglePrior)
```

---

<code>get.cumulative</code>	<i>Cumulative triangle</i>
-----------------------------	----------------------------

---

**Description**

Switch from an incremental to a cumulative triangle

**Usage**

```
get.cumulative( triangle )
```

**Arguments**

triangle      An incremental run-off triangle

**Value**

The cumulative triangle

**Note**

The methods in this the DCL package works normally on incremental triangles

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**See Also**

[get.incremental](#)

**Examples**

```
data(NtriangleDCL)
get.cumulative(NtriangleDCL)
```

---

get.incremental      *Incremental triangle*

---

**Description**

Switch from an cumulative to an incremental triangle

**Usage**

```
get.incremental( triangle )
```

**Arguments**

triangle      A cumulative run-off triangle

**Value**

The incremental triangle

**Note**

The methods in this the DCL package works normally on incremental triangles



**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**See Also**

[get.cumulative](#)

**Examples**

```
data(NtriangleDCL)
Ntriangle.cum<-get.cumulative(NtriangleDCL)
get.incremental(Ntriangle.cum)
```

---

idcl. estimation	<i>Parameter estimation - DCL model reproducing the incurred reserve.</i>
------------------	---

---

**Description**

Estimate the parameters in the Double Chain Ladder model model: delay parameters, severity mean and variance. The inflation parameter is corrected using the incurred data to provide the incurred cashflow.

**Usage**

```
idcl. estimation( Xtriangle , Ntriangle , Itriangle , adj = 1 ,
  Tables = TRUE , num. dec = 4 , n. cal = NA ,
  Fj.X = NA , Fj.N = NA , Fj.I = NA)
```

**Arguments**

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
Itriangle	The incurred triangle. It should be a matrix with incurred data located in the upper triangle. It is an incremental run-off triangle with the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
adj	Method to adjust the estimated delay parameters for the distributional model. It should be 1 (default value) or 2. See more in details below.
Tables	Logical. If TRUE (default) it is showed a table with the estimated parameters.
num. dec	Number of decimal places used to report numbers in the tables (if Tables=TRUE).

n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).
Fj.X	Optional vector with length m-1 (m being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from Xtriangle. See more details in <a href="#">clm</a> .
Fj.N	Optional vector with length m-1 with the development factors to calculate the chain ladder estimates from Ntriangle.
Fj.I	Optional vector with length m-1 with the development factors to calculate the chain ladder estimates from Itriangle.

### Details

Two model are estimated in the double chain ladder framework as with the `dcl. estimation` function. In this case the DCL inflation parameter estimated by `dcl. estimation` from `Ntriangle` and `Xtriangle` is adjusted so that the derived predicted reserve is equal to the incurred reserve. Use this estimation method if you want the RBNS/IBNR split the incurred reserve and the incurred full cashflow.

### Value

pi.delay	General delay parameters
mu	Mean severity factor
inflat	Underwriting severity inflation (BDCL inflation)
inflat.DCL	Underwriting severity inflation (DCL inflation)
pj	Delay probabilities (under a Multinomial assumption)
mu.adj	Adjusted mean factor corresponding to the pj parameters
sigma2	Variance severity factor
phi	Overdispersion parameter used to derive the estimate sigma2
Ey	Severity mean for each underwriting period
Vy	Severity variance for each underwriting period
adj	Type of adjusted used to derive the pj probabilities
alpha.N	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle (Ntriangle)
beta.N	Underwriting chain ladder parameter in the (OD)-Poisson model. Counts triangle (Ntriangle)
Nhat	The chain ladder predictions (counts triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
alpha.X	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle (Xtriangle)
beta.X	Underwriting chain ladder parameter in the (OD)-Poisson model. Paid triangle (Xtriangle)

Xhat	The chain ladder predictions (paid triangle). It is a matrix having the chain ladder predictions in the future (lower triangle) and the fitted values in the past (upper triangle).
alpha.I	Underwriting chain ladder parameter in the (OD)-Poisson model. Incurred triangle (Itriangle)
beta.I	Underwriting chain ladder parameter in the (OD)-Poisson model. Incurred triangle (Itriangle)
CL.I.i	Outstanding incurred numbers (row sums of the lower predicted triangle) from classical chain ladder on the incurred triangle.

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

### References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76. Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.

### See Also

[Plot.dcl.par](#), [dcl.predict](#), [dcl. estimation](#), [bdcl. estimation](#)

### Examples

```
data(NtriangleBDCL)
data(XtriangleBDCL)
data(ItriangleBDCL)

my.idcl.par<-idcl. estimation(XtriangleBDCL,NtriangleBDCL,ItriangleBDCL)
# Parameters
Plot.dcl.par(my.idcl.par,type.inflat='IDCL')
# IDCL Predictions by diagonals (future calendar years)
preds.idcl.diag<-dcl.predict(my.idcl.par,NtriangleBDCL,num.dec=0)

# Comparing with the BDCL method
my.bdcl.par<-bdcl. estimation(XtriangleBDCL,NtriangleBDCL,ItriangleBDCL)
# Parameters shown in Table 1
Plot.dcl.par(my.bdcl.par,type.inflat='BDCL')
# BDCL Predictions by diagonals (future calendar years)
preds.bdcl.diag<-dcl.predict(my.bdcl.par,NtriangleBDCL,num.dec=0)
```

---

ItriangleBDCL

*Incurred data (BDCL example)*


---

### Description

Real motor data from a major insurer. It is a yearly run-off (incremental) triangle consisting of the incurred data during 19 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen and Verrall (2013).

### Usage

```
data(ItriangleBDCL)
```

### Format

Matrix with dimension 19 by 19: 19 undewriting years and 19 development years.

### References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Fergusson. *North American Actuarial Journal*, 17(2), 101-113.

### Examples

```
data(ItriangleBDCL)
data(XtriangleBDCL)
m<-nrow(XtriangleBDCL)

clm.I<-clm(ItriangleBDCL)
alpha.I<-clm.I$alpha
# The total paid for each accident year in the past
Ri.X<-rowSums(XtriangleBDCL,na.rm=TRUE)
# Incurred outstanding numbers
Ri.CL.incurred<-alpha.I-Ri.X
Total.CL.incurred<- sum(Ri.CL.incurred,na.rm=TRUE)

## Compare with CL on paid data
clm.X<-clm(XtriangleBDCL)
Xhat<-as.matrix(clm.X$triangle.hat)
Ri.CL.paid<-rowSums(Xhat)-rowSums(XtriangleBDCL,na.rm=TRUE)
Total.CL.paid<- sum(Ri.CL.paid,na.rm=TRUE)

# the predictions by rows
data.frame(underw.year=c(1:m,"Total"),CLM.paid=c(Ri.CL.paid,Total.CL.paid),
           CLM.incurred=round(c(Ri.CL.incurred,Total.CL.incurred),4))

# now the predictions by diagonals
inflat.factor<-Ri.CL.incurred/Ri.CL.paid
inflat.factor[Ri.CL.paid==0]<-1
```

```

# the lower triangle from incurred chain ladder is defined as:
Ihat<-Xhat
for (i in 1:m) Ihat[i,]<-Xhat[i,]*inflat.factor[i]
# now the sums by diagonals
Diag.CL.paid<-sapply(split(Xhat, row(Xhat)+col(Xhat)), sum, na.rm=TRUE)
Dclm.paid<-c(Diag.CL.paid[-(1:m)])
Total.CL.paid<- sum(Dclm.paid,na.rm=TRUE)
Dclm.paid<-c(Dclm.paid,Total.CL.paid)

Diag.CL.inc<-sapply(split(Ihat, row(Ihat)+col(Ihat)), sum, na.rm=TRUE)
Dclm.inc<-c(Diag.CL.inc[-(1:m)])
Total.CL.inc<- sum(Dclm.inc,na.rm=TRUE)
Dclm.inc<-c(Dclm.inc,Total.CL.inc)

# A table with the chain ladder predictions (paid and incurred data)
data.frame(Future.years=c(1:(m-1),'Tot.'),
           clm.paid=round(Dclm.paid),clm.incurred=round(Dclm.inc))

```

---

NpaidPrior

*Number of non-zero payments (adding prior knowledge example)*


---

### Description

It is a yearly run-off (incremental) triangle consisting of the number of non-zero payments during 14 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013).

### Usage

```
data(NpaidPrior)
```

### Format

Matrix with dimension 14 by 14: 14 undewriting years and 14 development years.

### Source

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

### Examples

```
data(NpaidPrior)
Plot.triangle(NpaidPrior)
```

---

NtriangleBDCL	<i>Number of reported claims (BDCL example)</i>
---------------	---

---

**Description**

Real motor data from a major insurer. It is a yearly run-off (incremental) triangle consisting of the number of reported claims during 19 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen and Verrall (2013).

**Usage**

```
data(NtriangleBDCL)
```

**Format**

Matrix with dimension 19 by 19: 19 undewriting years and 19 development years.

**References**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Fergusson. *North American Actuarial Journal*, 17(2), 101-113.

**Examples**

```
data(NtriangleBDCL)

Plot.triangle(NtriangleBDCL, Histogram=TRUE)
Plot.triangle(NtriangleBDCL)

# Classical chain ladder method
clm(NtriangleBDCL)
```

---

NtriangleDCL	<i>Number of reported claims (DCL example)</i>
--------------	--

---

**Description**

Real motor data from a major insurer. It is a yearly run-off (incremental) triangle consisting of the number of reported claims during 10 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen and Verrall (2012).

**Usage**

```
data(NtriangleDCL)
```

**Format**

Matrix with dimension 10 by 10: 10 undewriting years and 10 development years.

**Source**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

**Examples**

```
data(NtriangleDCL)

Plot.triangle(NtriangleDCL, Histogram=TRUE)
Plot.triangle(NtriangleDCL)

# Classical chain ladder method
clm(NtriangleDCL)
```

---

NtrianglePrior	<i>Number of reported claims (adding prior knowledge example)</i>
----------------	---

---

**Description**

It is a yearly run-off (incremental) triangle consisting of the number of reported claims during 14 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013).

**Usage**

```
data(NtrianglePrior)
```

**Format**

Matrix with dimension 14 by 14: 14 undewriting years and 14 development years.

**Source**

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

**Examples**

```
data(NtrianglePrior)

Plot.triangle(NtrianglePrior, Histogram=TRUE)
Plot.triangle(NtrianglePrior)

# Classical chain ladder method
clm(NtrianglePrior)
```

---

`Plot.cashflow`*Plotting the full cashflow (bootstrap distribution)*

---

### Description

Provide histograms and boxplots of the RBNS, IBNR and total(=RBNS+IBNR) cashflows. The boxplots corresponds to the distribution of the outstanding liabilities in the future calendar periods. The histograms show the distribution of the reserve (overall total).

### Usage

```
Plot.cashflow( cashflow )
```

### Arguments

`cashflow` A list object returned by the function `dcl.boot` or `dcl.boot.prior`.

### Details

The cashflow should be derived by specifying the parameter `summ.by="diag"` in the function `dcl.boot` or `dcl.boot.prior`.

### Value

No returned value.

### Author(s)

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

### References

- Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.
- Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.
- Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

### See Also

[dcl.boot](#), [dcl.boot.prior](#), [dcl.estimation](#)



**Examples**

```
# Results described in the data application by Martinez-Miranda, Nielsen and Verrall (2012)
data(NtriangleDCL)
data(XtriangleDCL)

# Estimation of the DCL parameters
est<-dcl.estimation(XtriangleDCL,NtriangleDCL)
# Full cashflow considering the tail (only variance process)
# Below only B=200 simulations for a fast example
boot1<-dcl.boot(dcl.par=est,Ntriangle=NtriangleDCL,boot.type=1,B=200)
Plot.cashflow(boot1)
```

---

Plot.clm.par

*Plotting the estimated chain ladder parameters*

---

**Description**

Show a plot with the estimates of the chain ladder parameters and the development factors

**Usage**

```
Plot.clm.par( clm.par )
```

**Arguments**

clm.par            A list object with the estimated chain ladder parameters: the value returned by the functions `clm`.

**Value**

No returned value

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

**See Also**

[clm](#), [dcl.estimation](#), [Plot.triangle](#)

**Examples**

```
data(NtriangleDCL)
my.clm.par<-clm(NtriangleDCL)

Plot.clm.par(my.clm.par)
```

---

Plot.dcl.par

*Plotting the estimated parameters in the DCL model*

---

**Description**

Show a two by two plot with the estimated parameters in the Double Chain Ladder model

**Usage**

```
Plot.dcl.par( dcl.par , type.inflat = 'DCL' )
```

**Arguments**

dcl.par	A list object with the estimated parameters: the value returned by the functions <code>dcl.estimation</code> , <code>bdcl.estimation</code> or <code>idcl.estimation</code> .
type.inflat	Method used to estimate the inflation . Possible values are: 'DCL' (default) if it was used <code>dcl.estimation</code> , 'BDCL' if <code>bdcl.estimation</code> , and 'IDCL' if <code>idcl.estimation</code>

**Value**

No returned value

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.

**See Also**

[dcl.estimation](#), [bdcl.estimation](#), [idcl.estimation](#)

**Examples**

```

data(NtriangleDCL)
data(XtriangleDCL)

# Estimation of the DCL parameters described in Martinez-Miranda, Nielsen and Verrall (2012)
my.dcl.par<-dcl.estimation(XtriangleDCL,NtriangleDCL)
Plot.dcl.par(my.dcl.par)

```

---

Plot.triangle	<i>Plotting an incremental run-off triangle</i>
---------------	---

---

**Description**

Graphical representaion of an incremental run-off triangle.

**Usage**

```
Plot.triangle( triangle , Histogram = FALSE , tit='' )
```

**Arguments**

triangle	The loss incremental triangle. It should be a matrix with the observed counts (number of reported claims, number of payments etc.), payments or incurred data, located in the upper triangle. The lower triangle consisting in missing or zero values.
Histogram	Logical. If TRUE then a histogram representing the triangle is shown. If FALSE (default) then a classical representation of the triangle is shown, this is, a matplot of the row sums from both incremental and cummulative triangle.
tit	Character. Title to be added to the plot

**Details**

A histogram representation of the histogram is consistent with the run-off triangles of counts such as the number of reported claims, number of payments, etc. See Martinez-Miranda, Nielsen, Sperlich and Verrall (2013) for a further explanation.

**Value**

No returned value

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

## References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

Martinez-Miranda M.D., Nielsen, J.P., Sperlich, S., Verrall, R. (2013). Continuous Chain Ladder: Reformulating and generalizing a classical insurance problem. *Experts Systems with Applications*, 40(14), 5588-5603.

## See Also

[get.incremental](#), [clm](#)

## Examples

```
## Plotting a counts triangle (number of reported claims)
data(NtriangleDCL)
Plot.triangle(NtriangleDCL, Histogram=TRUE, tit=expression(paste('Counts: ', N[ij])))
# Classical CL predictions
clm.N<-clm(NtriangleDCL)
Nhat<-clm.N$triangle.hat
# Compare the original histogram with the CL projections
Plot.triangle(Nhat, Histogram=TRUE, tit='CL Predictions')

## Plotting a paid triangle (number of reported claims)
data(XtriangleDCL)
Plot.triangle(XtriangleDCL)
```

---

validating.incurred      *Back-test: testing against the experience*

---

## Description

A back-test to validate incurred reserve (IDCL) against paid reserve (DCL) or the paid with a Bornhuetter-Fergusson adjustment (BDCL). The validation strategy consists of: (1) Cut  $ncut=1,2,..$  diagonals from the observed paid triangle. (2) Apply the three methods (DCL, BDCL and IDCL), and (3) compare forecasts and actual values.

## Usage

```
validating.incurred( ncut = 0 , Xtriangle , Ntriangle , Itriangle ,
  Model = 0 , Plot.box = TRUE , Tables = TRUE , num.dec = 4 ,
  n.cal = NA , Fj.X = NA , Fj.N = NA , Fj.I = NA)
```

## Arguments

**ncut**                      The number of last periods (diagonals) to cut from the paid triangle. The default value is 0 (see details below).

Xtriangle	The paid run-off triangle: incremental aggregated payments. It should be a matrix with incremental aggregated payments located in the upper triangle and the lower triangle consisting in missing or zero values.
Ntriangle	The counts data triangle: incremental number of reported claims. It should be a matrix with the observed counts located in the upper triangle and the lower triangle consisting in missing or zero values. It should has the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
Itriangle	The incurred triangle. It should be a matrix with incurred data located in the upper triangle. It is an incremental run-off triangle with the same dimension as Xtriangle (both in the same aggregation level (quarters, years,etc.))
Model	Possible values are 0, 1 or 2 (default). See more details below.
Plot.box	Logical. If TRUE (default) it is shown a boxplot of the errors in the cells predic-tions.
Tables	Logical. If TRUE (default) it is shown a table with the errors in the cells, diago-nals and overall total prediccion.
num.dec	Number of decimal places used to report numbers in the tables. Used only if Tables=TRUE.
n.cal	Integer specifying the number of most recent calendars which will be used to calculate the development factors. By default n.cal=NA and all the observed calendars are used (classical chain ladder).
Fj.X	Optional vector with lentgth m-1 (m being the dimension of the triangles) with the development factors to calculate the chain ladder estimates from Xtriangle. See more details in <a href="#">clm</a> .
Fj.N	Optional vector with lentgth m-1 with the development factors to calculate the chain ladder estimates from Ntriangle.
Fj.I	Optional vector with lentgth m-1 with the development factors to calculate the chain ladder estimates from Itriangle.

## Details

If  $ncut=0$  the test is not computed but a plot showing the difference among the three methods is shown. It is recommended to start with this step to have some insight about the problem. Note that the first part in the IDCL inflation is usually very volatile since no many outstanding liabilities arise from the first underwriting periods.

The prediction errors provided through the value `pe` vector are calculated as follow:

For individual cells:  $pe.cells = \text{sum}(ce.dif^2) / \text{sum}(ce.obs^2)$

with `ce.dif` being the vector with the differences between the predicted cells and the actual cells (`ce.obs`).

For diagonals:  $pe.diags = \text{sum}(ca.dif^2) / \text{sum}(ca.obs^2)$

with `ca.dif` being the vector with the differences between the predicted calendars and the actual calendars (`ca.obs`).

For the total reserve:  $pe.tot = \text{sum}(tot.dif^2) / \text{sum}(tot.obs^2)$

with `tot.dif` the absolute difference between the predicted reserve and the actual reserve (`tot.obs`).

**Value**

pe.vector	A vector (length 10) with elements being (in the following order): ncut, the averaged errors predicting cells by DCL, BDCL and IDCL (see pe.cells in Details above), the three averaged errors by predicting diagonals (pe.diags), and the three errors by predicting the overall total (pe.tot).
Xdif	A matrix with the individual cells errors (see ce.dif in Details above) for each method (by columns)
Inflat.DCL	The estimated underwriting DCL inflation using <a href="#">dcl. estimation</a> . Only provided if ncut=0.
Inflat.BDCL	The estimated underwriting BDCL inflation using <a href="#">bdcl. estimation</a> . Only provided if ncut=0.
Inflat.IDCL	The estimated underwriting IDCL inflation using <a href="#">idcl. estimation</a> . Only provided if ncut=0.

**Note**

To validate classical chain ladder on paid data against classical chain ladder on incurred data it should be used `Model=0` (see [dcl.predict](#)) for more details.

**Author(s)**

M.D. Martinez-Miranda, J.P. Nielsen and R. Verrall

**References**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.

Martinez-Miranda M.D., Nielsen, J.P., Sperlich, S., Verrall, R. (2013). Continuous Chain Ladder: Reformulating and generalizing a classical insurance problem. *Experts Systems with Applications*, 40(14), 5588-5603.

**See Also**

[dcl. estimation](#), [bdcl. estimation](#), [idcl. estimation](#), [,dcl.predict](#)

**Examples**

```
data(NtriangleBDCL)
data(XtriangleBDCL)
data(ItriangleBDCL)

Ntriangle<-NtriangleBDCL
Xtriangle<-XtriangleBDCL
Itriangle<-ItriangleBDCL
## First compare the three methods to be validated (three different inflations)
validating.incurred(ncut=0,Xtriangle,Ntriangle,Itriangle)

## Now perform a backtest cutting up to four calendars backward
```

```

test.res<-matrix(NA,4,10)
par(mfrow=c(2,2),cex.axis=0.9,cex.main=1)
par(mar=c(1.5,1.5,1.5,1.5),oma=c(1,0.5,0.5,0.2),mgp=c(3,0.5,0))
for (i in 1:4)
{
  res<-validating.incurred(ncut=i,Xtriangle,Ntriangle,Itriangle,Tables=FALSE)
  test.res[i,]<-as.numeric(res$pe.vector)
}
test.res<-as.data.frame(test.res)
names(test.res)<-c("num.cut","pe.point.DCL","pe.point.BDCL","pe.point.IDCL",
"pe.calendar.DCL","pe.calendar.BDCL","pe.calendar.IDCL",
"pe.total.DCL","pe.total.BDCL","pe.total.IDCL")
print(test.res)

```

---

XtriangleBDCL

*Paid data (BDCL example)*


---

### Description

Real motor data from a major insurer. It is a run-off (incremental) triangle consisting of the aggregated payments during 19 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen and Verrall (2013).

### Usage

```
data(XtriangleBDCL)
```

### Format

Matrix with dimension 19 by 19: 19 undewriting years and 19 development years.

### References

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2013) Double Chain Ladder and Bornhuetter-Ferguson. *North American Actuarial Journal*, 17(2), 101-113.

### Examples

```

data(XtriangleBDCL)

Plot.triangle(XtriangleBDCL)
# Classical chain ladder method
clm(XtriangleBDCL)

```

---

`XtriangleDCL`*Paid data (DCL example)*

---

**Description**

Real motor data from a major insurer. It is a yearly run-off (incremental) triangle consisting of the aggregated payments during 10 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen and Verrall (2012).

**Usage**

```
data(XtriangleDCL)
```

**Format**

Matrix with dimension 10 by 10: 10 undewriting years and 10 development years.

**Source**

Martinez-Miranda, M.D., Nielsen, J.P. and Verrall, R. (2012) Double Chain Ladder. *Astin Bulletin*, 42/1, 59-76.

**Examples**

```
data(XtriangleDCL)
Plot.triangle(XtriangleDCL)
# Classical chain ladder method
clm(XtriangleDCL)
```

---

`XtrianglePrior`*Paid data (adding prior knowledge example)*

---

**Description**

It is a run-off (incremental) triangle consisting of the aggregated payments during 19 years. These data were used in the empirical illustration provided by Martinez-Miranda, Nielsen, Verrall and Wuthrich (2013).

**Usage**

```
data(XtrianglePrior)
```

**Format**

Matrix with dimension 14 by 14: 14 undewriting years and 14 development years.



**Source**

Martinez-Miranda, M.D., Nielsen, J.P., Verrall, R. and Wuthrich, M.V. (2013) Double Chain Ladder, Claims Development Inflation and Zero Claims. *Scandinavian Actuarial Journal*. In press.

**Examples**

```
data(XtrianglePrior)

Plot.triangle(XtrianglePrior)
# Classical chain ladder method
clm(XtrianglePrior)
```

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